

Evolution of periodicity in periodical cicadas

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THESIS

EVOLUTION OF PERIODICITY IN
PERIODICAL CICADAS

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THESIS

EVOLUTION OF PERIODICITY IN
PERIODICAL CICADAS

周期ゼミの周期性進化メカニズムの解明

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Abstract

Periodical cicadas (*Magicicada* spp.) in the USA are famous for their unique prime-numbered life cycles of 13 and 17 years and their nearly perfectly synchronized mass emergences. Because almost all known species of cicada are non-periodical, periodicity is assumed to be a derived state. Cicadas (Order: Hemiptera) are singing insects that are widely distributed from the tropics to temperate zones. Almost all known cicada species have size (weight)-dependent maturation with variable-length life cycles. Their nymphs grow underground at a rate set by resource availability (water from roots that depends on the cumulative temperatures of trees), and when they reach a threshold maturation size, they emerge from the ground and moult into short-lived adults. In contrast, *Magicicada* exhibit time-dependent maturation and emerge after exactly 13 or 17 years. In the current climate (postglacial period), most of them appear to be able to grow to threshold maturation size well within their lifespans of 13 or 17 years. A number of hypotheses address the evolution and maintenance of periodicity and mass emergence in *Magicicada*. One hypothesis is that periodicity with mass emergence is a strategy for predator avoidance, but this hypothesis has a significant flaw: It cannot account for the rarity of periodicity. All cicadas face predation pressure, but only a small number of species are known to be periodical. A leading hypothesis for the evolution of periodicity in *Magicicada* implicates the decline in average temperature during glacial periods. During ice ages, the emergence of any cicadas with size-dependent life cycles may have been delayed many years due to the reduction in yearly cumulative temperatures. It is possible that the long nymphal stage preceding such emergence delays could have significantly increased nymphal mortality, resulting in extremely low adult densities. One way that the ancestors of *Magicicada* may have survived these challenges was by adopting periodical emergences. During the evolution of periodicity, the determinant of maturation in ancestral cicadas is hypothesized to have switched from size dependence to time (period)

dependence. The selection for the prime-numbered cycles should have taken place only after the fixation of periodicity. Here, we build a simple individual-based model of cicadas which incorporates Mendelian inheritance and random mutation under conditions of climatic cooling to explore the fixation of periodicity. We assume a one-locus, two-allele genetic system controlling emergence (i.e., determinant of maturation). In this locus, we assume two types of alleles: (1) temperature (size)-dependent alleles and (2) time-dependent alleles (i.e., temperature-independent or periodicity alleles) that have a specific lifespan length (e.g., 10-20 years). In this paper, we specifically demonstrate how declining average temperature, which directly affects growth rate, could promote the evolution of time-dependent maturation and periodicity from an ancestor with size-dependent maturation. There is a border of extinction such that if the climate is cooler than the threshold, the population usually goes extinct. If the climate is warmer than this threshold, cicadas survive in almost all simulation runs. Periodicity is fixed at and near the boundary of extinction. A wide band of fixed periodicity is found slightly below the boundary of extinction, where the shorter (longer) cycles are fixed at warmer (cooler) cumulative temperatures. Our simulation demonstrates the feasibility of the first step of Yoshimura's (1997) hypothesis for the evolution of periodicity during glacial periods. Our results indicate that various year cycles (10-20 year) could have evolved depending on slight differences in accumulated temperatures. In our model, under cold environments, extremely long juvenile stages lead to extremely low adult densities, limiting mating opportunities and favouring the evolution of synchronized emergence. Our results indicate that these changes, which were triggered by glacial cooling, could have led to the fixation of periodicity in the nonperiodical ancestors.

Doctoral Dissertation Table of Contents

Hiromu Ito

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1. Introduction

True periodicity, involving synchronized adult emergences, fixed life-cycle lengths, and intervals between emergences with no adults present, is rare among insects [1]. The periodical cicadas of eastern North America (*Magicicada* spp.) exhibit 17- and 13-year periodical life cycles, the most extreme periodical life cycles known in insects [2-6]. *Magicicada* are also characterized by mass emergences and division into regional populations that share emergence years. In periodical cicadas, each “emergence year-class” is specifically called a “brood” [2, 3]. Cicadas (Order: Hemiptera) are singing insects that are widely distributed from the tropics to temperate zones. Almost all known cicada species have size (weight)-dependent maturation with variable-length life cycles. Their nymphs grow underground at a rate set by resource availability (water from roots that depends on the cumulative temperatures of trees), and when they reach a threshold maturation size, they emerge from the ground and moult into short-lived adults [7, 8].

In contrast, *Magicicada* exhibit time-dependent maturation and emerge after exactly 13 or 17 years. In the current climate (postglacial period), most of them appear to be able to grow to threshold maturation size well within their lifespans of 13 or 17 years [9]. However, some small, under-developed adults are occasionally found. This observation means that *Magicicada* emerge after a fixed length of time, irrespective of reaching a threshold body size. Thus, a prominent question regarding the evolution of periodical cicadas is why they transitioned from size-dependent to time-dependent maturation [10, 11].

A number of hypotheses address the evolution and maintenance of periodicity and mass emergence in *Magicicada*. One hypothesis is that periodicity with mass emergence is a strategy for predator avoidance [12-15], but this hypothesis has a significant flaw: It cannot account for the rarity of periodicity. All cicadas face predation pressure, but only a small number of species are known to be periodical, e.g., one in India [16, 17] and another in Fiji

[18]. Other hypotheses suggest that geological cooling during glacial periods triggered the evolution of periodical cicadas [19, 20], but these hypotheses are also limited because many species of cicadas live in glaciated areas, yet only a few are periodical. The unique combination of natural history traits in *Magicicada* argues for an explanation that divides the evolution of *Magicicada* into smaller problems.

One focus of *Magicicada* studies has been on the relationship between the mass emergence of these species and the unusual, prime-numbered life cycles of 13 or 17 years. However, the persistence of prime-numbered cycles has been shown to be a plausible outcome of circumstances in which already-periodical cicadas face disproportionately high predation pressures when they emerge at low densities [14, 21-23]. Moreover, repeated instances of life-cycle switching from 13 to 17 years or vice versa over evolutionary time [24] suggest that these life cycles are stable strategies, whereas other alternatives are not.

The history of periodical cicadas involves periods of confinement in forested refugia when other regions of the eastern half of North America were still directly or indirectly rendered unsuitable by glaciation. During ice ages, the emergence of any cicadas with size-dependent life cycles may have been delayed many years due to the reduction in yearly cumulative temperatures. It is possible that the long nymphal stage preceding such emergence delays could have significantly increased nymphal mortality, resulting in extremely low adult densities. Furthermore, populations may have been vulnerable to extinction due to several factors, including limited mating opportunities, severe predation pressure, and high mortality under marginal climate conditions [23, 25].

One way that the ancestors of *Magicicada* may have survived these challenges was by adopting periodical emergences. When geological cooling advances, average juvenile

(nymphal) period elongates, and at the same time the variation in juvenile growth period increases, resulting to an extremely low adult density. First, consider the elongation of juvenile period as follows. Suppose the ancestral cicadas emerge every year and the growth period is about 7 years with 100 adult individuals emerging in a small habitat. This means a total of 700 (100×7 year) adults emerging in 7 years. Next, cooling arrives and doubles the growth period to 14 years. If we assume that the overall mortality per nymph is identical, 700 individuals emerging in 14 years means 50 adult individuals per year. However, this nymphal mortality should be incorrect. Otherwise, nymphal mortality per year is halved since the nymphal stage is doubled. Assuming the nymphal mortality per year is constant, the emerging adult population size becomes 25 individuals per year (total population size is $25 \times 14 = 350$ individuals). Thus, under the same mortality condition, the adult density per year should be quartered (i.e., $1/4$). However, geological cooling should drastically increase the annual juvenile mortality due to freezing and desiccation. Thus the resulting yearly adult population size becomes exceptionally small compared with those before geological cooling.

Geological cooling also reduces the adult density by increasing the variation in juvenile growth rates. For example, the variation in yearly emergence should increase significantly when the average yearly emergence is 5 individuals compared with 100 individuals.

Therefore, the adult emergence may become vacant in most years, resulting to periodical emergence even under size-dependent maturation. Moreover, when the population size at a given year reaches a critically low density, the emergence of adult individuals should become almost periodical and nearly synchronized, even under size-dependent maturation. In this stage, the variation in juvenile growth further boosts adult density because of the loss of adults emerging in a wrong (previous or next) year. For example, when non-periodical adults lay one hundred eggs, some eggs (say 10) grow faster, resulting in one-year early emergence; while some others (say 10) are slower, resulting in one-year late emergence. These early and

late emergences (total 20 adults) can be lost without producing any offspring. Because of this, adult density is reduced by 80% in every generation. By switching to periodical emergence with a fixed period (complete synchronization), this loss of emergence disappears. We hypothesize that this advantage of periodical emergence over size-dependent maturation can lead to the evolution (fixation) of periodical genes, during cooling, so that the population is at a lower risk of extinction.

In this paper, we specifically demonstrate how declining average temperature, which directly affects growth rate, could promote the evolution of time-dependent maturation and periodicity from an ancestor with size-dependent maturation. Under climatic cooling conditions, our model suggests that size-dependent cicadas could be replaced by periodical cicadas with life cycles of various year lengths. In our model runs, cicadas that acquire periodicity establish only one brood when the Allee effects are moderately strong. Slight variations in conditions affect model outcomes: cooler temperatures promote the establishment of longer cycles, while warmer temperatures promote the establishment of shorter cycles. Our results provide insights concerning the initial conditions necessary to provide a selective advantage for periodicity in North American *Magicicada*.

2. Model

2.1. Individual based model (IBM)

We build a simple individual-based model incorporating Mendelian inheritance and random mutation (Fig. 1, see supplementary information). We assume a one-locus, two-allele genetic system controlling emergence (i.e., determinant of maturation). In this locus, we assume two types of alleles: (1) temperature (size)-dependent alleles and (2) time-dependent alleles (i.e., temperature-independent or periodicity alleles) that have a specific lifespan length (e.g., 10-20 years). Alleles for periodicity of any given year cycle length are assumed to be dominant, whereas the temperature-dependent allele (ancestral allele) is recessive.

An average temperature (T_{mean} , in an arbitrary unit) is set for each simulation with a value between 17.0 and 20.0 (0.1 intervals). In each simulation, the yearly temperature fluctuates following the discretized and truncated normal distribution of the integer type obtained from the Gaussian random variables with mean= T_{mean} and standard deviation=0.5 (Fig. S1). We start with the values of the Gaussian probability density function at each integer (from -3 to +3) and then scale them up so that they add up to one. Here discretization and truncation save memory size and simulation time considerably because we only calculate seven integer cases. We expect no qualitative changes with these modifications. The maximum and minimum temperatures are $T_{mean} \pm 3$. The yearly temperatures have no time correlation (i.e., are independent from each other).

In the original setting, we assume that the ancestral non-periodical cicadas die if they cannot reach maturity by a certain period. An introduced mutant allele is set with this period length. For example, if 10 years are necessary for maturation, the introduced mutant has a 10-year

period. Accordingly, when we test the fixation of the 10-year allele, we assume that all non-periodical cicadas die if they do not reach maturation in 10 years. This is rather a severe disadvantage for non-periodical cicadas because they cannot survive over the fixed period length. However, because the climatic conditions during the glacial periods are severe, increasing the juvenile period, juvenile mortality must be increased. Therefore, a periodicity allele should be fixed at the verge of extinction. Nevertheless, this setting might provide a large advantage over non-periodical ancestors. Therefore, we also test the case where this limitation is absent.

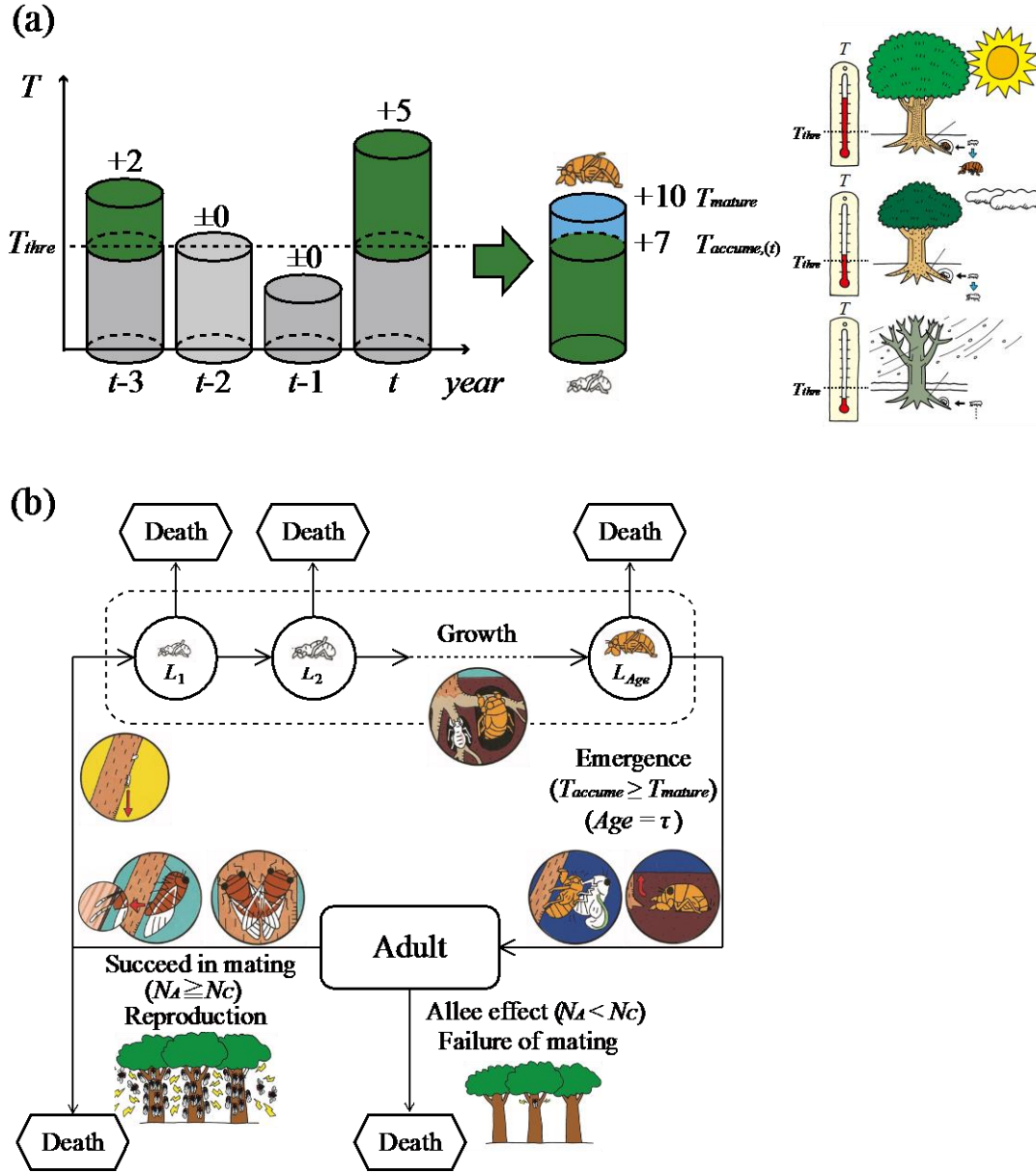


Fig. 1. Illustration of the individual-based model (IBM). (a) Image of the accumulated temperature. The area in green above T_{thre} represents growth based on accumulated temperature. When the sum of accumulated temperature (T_{accume}) reaches the threshold amount for maturation (T_{mature}), the non-periodical cicadas emerge. (b) Simulation flow. The variable T_{thre} is defined as the temperature threshold of individual cicada i , such that if $T_t \leq T_{thre,i}$ (for some t), then $T_{mature,i}$ is fixed, resulting in a longer time of emergence. An individual cicada nymph $i(t)$ emerges at time t if $T_{accume, i(t-1)} \geq T_{mature}$. If $T_{accume, i(t-1)} < T_{mature}$, a nymph cannot emerge the next year. Illustration by Yoshihiko Ishimori.

2.1.1. Nymphal growth and accumulated temperatures

Nymphal growth is dependent on accumulated temperatures that are closely correlated with tree growth [7]. Trees grow when the ambient temperature is warmer than their growth limits. The amount of tree growth depends on the difference between the average ambient temperature and the tree growth limit. The yearly growth of trees thus depends on the sum of monthly (or daily) differences accumulated over the year. This sum of the temperatures is often called the effective accumulated (accumulative) temperature. This correlation between tree growth and ambient temperature is suspected to be attributable to water uptake. The water uptake of a tree is expected to cease when the ambient temperature is below the growth limit. Therefore, the rate of tree growth is correlated with the amount of water uptake, which in turn depends on the difference between the average ambient temperature and the tree growth limit.

Here, the amount of cicada growth must also depend on the amount of water taken up by trees because cicadas feed on tree roots. Thus, similar to growth in trees, the growth of cicada nymphs should depend on the accumulated temperatures. Furthermore, the growth limit of a tree should also be variable depending on the microenvironment. If a tree is situated on a south-facing slope, it grows even if the ambient temperature is relatively cold. However, on a north-facing slope, it ceases to grow even if the ambient temperature is relatively warm. Therefore, the growth of an individual cicada depends on the microenvironment of the trees it feeds on.

To model climate cooling, we introduce the concept of various temperature variables and parameters.

Here we introduce the concept of lower yearly temperature limit for positive growth for each individual, $T_{thre, i}$. This means that there are individual variations in both their own growth

ability and habitat they location in the yearly temperature threshold of the individual i , $T_{thre, i}$. An individual cicada nymph grows if $T > T_{thre, i}$. We express $T_{thre-average}$ as the average of $T_{thre, i}$. We also define T_{mean} , as the average ambient temperature. Then the average relative temperature (ART) is defined as $ART = T_{mean} - T_{thre-average}$. Note that, when $ART = 0$, the cicada growth rate is zero (i.e., the cicadas do not grow; Fig. 1a). For each individual, we calculate the sum of the yearly accumulated temperature in the year t of individual i ($T_{accume, i(t)}$) from the following equation.

$$T_{accume, i(t)} = T_{accume, i(t-1)} + T_{i, (t)} \quad (1)$$

where

$$T_{i, (t)} = \begin{cases} T_{(t)} - T_{thre, i} & \text{if } T_{(t)} \geq T_{thre, i} \\ 0 & \text{if } T_{(t)} < T_{thre, i} \end{cases} \quad (2)$$

The above variations in the monthly accumulated temperature can be accounted for by the variations in both the temporal environments and the individuals. The individual nymphs mature when the sum of the accumulated temperatures ($T_{accume, i(t)}$) reaches the threshold amount for maturation (T_{mature}). When nymphs reach a cumulative threshold nymphal size, such that $T_{accume, i(t-1)} \geq T_{mature}$, they emerge from the ground to become adults. To simulate cold glacial periods, the effective temperatures are set to extremely low levels; as a result, cicada growth to reach emergence size is slow. We observe whether the periodicity allele is fixed in the cicada populations (Fig. 1b). Because mutation is a rare event, we introduce a single period allele per simulation run (i.e., not two or more). Therefore, the words 'fixed' and 'fixation' are used specifically to mean the acquisition of periodicity (an introduced period allele). Adult cicadas are exposed to the Allee effect, a negative density effect at an extremely low density. We assume that adult populations $N_A(t)$ cannot reproduce below the critical population size N_c .

Thus, we set the growth limit of a cicada based on a yearly temperature threshold (T_{thre}). The cicada nymphs do not grow if the yearly accumulated temperature is below the yearly

temperature threshold. There are no additional costs to no growth beyond the yearly mortality and the loss of a year (time). We also introduce the variability of T_{thre} as follows. The average of the yearly temperature threshold is set to 19, and the variability is $T_{thre-average} \pm 2$ with equal probabilities, such that $T_{thre}=17, 18, 19, 20$ and 21 , with probability=0.2 for each. Note that the range of ambient temperature variation is set to be ± 3 from the average. Because yearly temperature variation represents large-scale climatic change, we assume that the local habitat variation (± 2) is smaller than the climatic change. A uniform distribution was chosen here to maintain a high variability in microhabitats and lower the computational loads of the program. We also test discretized and truncated normal distributions with high and low variability (standard deviation=0.5 and 1.0, respectively) as follows. We start with the values of the Gaussian probability density function at each integer ($T_{thre}=17, 18, 19, 20$, and 21) and then scale them up so that they add up to one (their summation equals one).

2.1.2. Maturity, emergence and penalty for insufficient growth

Individual nymphs mature when the sum of the accumulated temperature ($T_{accume, i(t)}$) reaches the threshold for maturation (T_{mature}). However, adult emergence differs between periodical and non-periodical cicadas. The ancestral non-periodical cicadas emerge in the year following maturation, such that an adult individual $i(t)$ emerges if $T_{accume, i(t-1)} \geq T_{mature}$. Here, we set $T_{mature}=10$. However, the periodical cicadas necessarily emerge at $Age=\tau$ (period, cycle), irrespective of their maturity ($T_{accume, i(t-1)}$). A female periodical cicada that emerges with insufficient accumulated temperature is penalized in the number of offspring, i.e., $T_{accume}(\tau) < T_{mature}=10$. We set the basic birth rate $b=10$ which is the maximum reproductive rate of non-periodical cicadas and matured periodical cicadas. Periodical cicadas with sufficient accumulated temperatures ($T_{accume, i(\tau)} \geq T_{mature} = 10$) keep the same birth rate with non-periodical cicadas, such that $b_{p,suff} = b$. The penalty in reproduction incurred by the

insufficient accumulated temperature is affected by the amount of shortage in accumulated temperature. Therefore, we assume maturity as the ratio of the accumulated temperature ($T_{accume,p,i}$) to the temperature necessary for maturation (T_{mature}), such that

$$b_{p,ins,i} = b \left(\frac{T_{accume,p,i}}{T_{mature}} \right) \quad (3)$$

2.1.3. Yearly nymphal mortality

All nymphs suffer from nymphal mortality every year. We set the yearly mortality with density effects such that

$$DR_{(t)} = 1 - \frac{1}{1 + \frac{\lambda-1}{k} N_{n,(t)}} \quad (\lambda > 1, k > 0) \quad (4)$$

where $DR_{(t)}$ is the mortality rate of year t , and N_n is the population size of the nymphs following the Beverton-Holt model [26]. We set the two model parameters ($\lambda=1.005$ and $k=250$; red line) for most simulation runs (Fig. S2). We also test the different parameter conditions (λ and k) because these parameters may be critical for the outcomes of the simulation. The original settings are used for these two parameters ($\lambda=1.005$ and $k=250$; red line) for most simulation runs (Fig. S2). Mortality may be affected by yearly temperatures, with lower temperatures increasing nymphal mortality. Freezing temperatures will not only reduce the root water flow available to the nymphs but also promote nymph desiccation, resulting in high nymph mortality. Therefore, we also vary these parameters to determine their effects. We first test various k values ($k=200, 250, 300$; supplementary Fig. S6). We assume that a cool environment has a low k parameter value ($=200$). In contrast, a warm environment has a high k ($=300$). We also vary λ ($\lambda=1.003, 1.005, 1.007$) (Fig. S6, S7).

2.1.4. Setup of individuals

Each individual is associated with the following information (trait values):

2.1.4.1. Periodicity alleles

The locus for the determinant of maturation has two different alleles: a temperature (size)-dependent allele (a) and a time-dependent (periodicity) allele (A). We assume that the periodicity allele (A) is dominant and the non-periodicity allele (a) is recessive. Therefore, individuals with AA and Aa genotypes emerge periodically, whereas those with aa genotypes emerge when their larval size exceeds a certain threshold (mature size). The genotypes of the ancestral cicadas are aa , and those of AA and Aa are periodical cicadas. We also evaluate the evolution of periodicity assuming that the periodicity allele is recessive and the non-periodicity allele is dominant. Simulation runs begin with all individuals having only temperature-dependent alleles; then, when the ancestral cicada population reaches a low stable density (step $t=1,000$), bidirectional mutation at the emergence locus is introduced at the rate of 0.001 per locus. We also test the case where the temperature-dependent allele is dominant under varying mutation rates (0.001 to 0.01).

When we introduce periodicity alleles, τ -year period is introduced for $\tau=10-20$. Within each simulation, only a single τ -year periodicity is introduced. We tested 10- to 20-year periods separately. The remaining year before emergence is also recorded for periodical cicadas. In the initial conditions, all individuals are set to have non-periodicity alleles. We introduced mutation at $t=1000$ (year) when the steady-state densities are reached. For each allele, bidirectional mutation is introduced at the birth of an individual at the rate of 0.001 from time step $t=1,000$ to the end of simulation steps ($a \leftrightarrow A$). We also run the simulation assuming one mutation per individual, such that no individual has a simultaneous double mutation (Fig. S11).

2.1.4.2. Age and virtual longevity

An egg has an age of zero years when it is deposited. Here, we assume that all non-periodical nymphs die if they do not reach maturity before the introduced period length (τ year). We also evaluate the effect of relaxing this condition by assuming that each individual nymph has the maximum virtual longevity of 50 years ($Age_{max}=50$ years). In warm climates, all cicadas should have emerged as adults or died before this age limit. However, in very cold climates, many nymphs never reach the adult stage and die with this 50-year age limit (see Fig. S3). The age (Age) of non-periodical cicadas ranges from 0 to 50, whereas that of periodical cicadas ranges from 0 to τ (τ , periodicity of emergence; $10 \leq \tau \leq 20$) because all periodical cicadas that reach maturity emerge as adults.

2.1.5. Simulation flow

The computer program is the individual-based model (IBM or multi-agent model), where all individuals are tracked during each time step. We only consider a female population and the corresponding male population is assumed to be identical, except for the penalty of birth rates, which is only associated with females. The simulation procedures are as follows:

- 1) Initially, we set the population size at 10,000 individuals, i.e., $N_A(t=0)=10,000$. All individuals are non-periodical cicadas with genotype aa .
- 2) Adult reproduction and nymphal growth are as follows:
 - (1) Adult cicadas mate and reproduce with a given birth rate. The birth rate is set as $b=10$ or as otherwise specified. All adults die immediately after reproduction.
 - (2) All eggs hatch immediately to become nymphs of age ‘zero’ years.
 - (3) The 0-year nymphs suffer no annual mortality.
 - (4) The nymphs of each age (L_{Age} for $Age=1, \dots, 49$) suffer from annual mortality DR .

- (5) The 50-year nymphs that do not reach maturity die before emerging as adults.
- (6) The mature nymphs emerge to become adults.
- (7) If the total number of emerging adults is less than the critical population size N_c , no reproduction takes place, resulting in extinction. However, if the total number exceeds N_c , return to step (1) and repeat the nymphal growth process for up to 999 time steps.
- 3) Upon the 1000th step, we introduce a bidirectional mutation between the periodicity and non-periodicity alleles (“A” $\leftrightarrow$ ”a”) in the offspring population at a mutation rate of 0.001 when reproduction takes place.
- 4) Emergence takes place as follows. Non-periodical nymphs emerge when they mature ($T_{accume, i}(t) \geq T_{mature} = 10$). Periodical nymphs become adults when they reach the given period (τ year). A female periodical cicada emerging with insufficient accumulated temperature ($T_{accume}(\tau) < T_{mature} = 10$) is given a discounted birth rate (i.e., $b_{p,ins,i}$).
- 5) Mating takes place at random among all emerged individuals. The genotypes of the offspring follow Mendelian inheritance.
- 6) Repeat steps 2) to 5) for an additional 9,000 time steps until $t=10,000$ or otherwise specified.

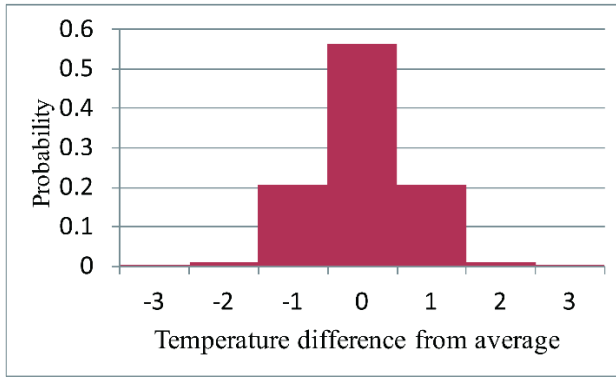


Fig.S1. Probability of yearly ambient temperature deviations from the average temperature. Bar graph expressing the event probability of a yearly temperature deviating from the average temperature.

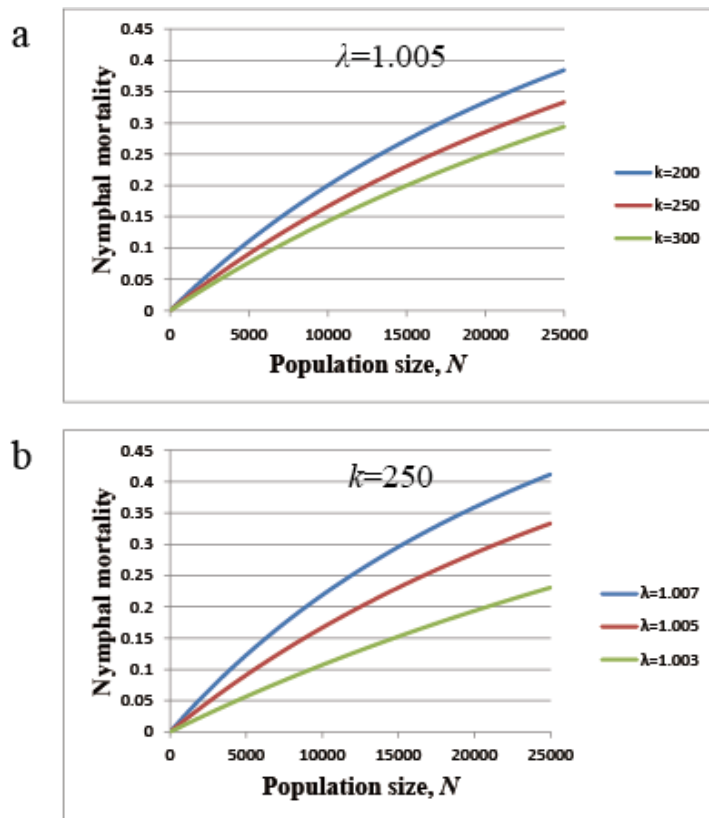


Fig.S2. Density-dependent nymphal mortality following the Beverton-Holt (1957) model with two parameters, λ and k . (a) A cool environment has a low k parameter value ($=200$). In contrast, a warm environment has a high k ($=300$). (b) A cool environment has a high λ ($=1.007$). In contrast, a warm environment has a low λ ($=1.003$).

3. Results

The simulation results show that fixation of the periodicity allele is frequently observed some time after the introduction of the mutation (Fig. 2). Here we show the population dynamics of a single simulation run. In a cooler climate ($ART=0$), temporal dynamics indicate that when the 10-year periodicity allele mutation is introduced at $t=1,000$ under the adult extinction threshold $N_c=100$, the fixation of periodicity occurs at $t=2,000$ (Fig. 2a). However, in a warm climate ($ART=+1$), no fixation is observed (Fig. 2b). When fixation occurs, the average adult population size increases approximately threefold, from less than 500 adults emerging annually to over 4,000 adults in a mass emergence (Fig. 2a). We also assessed the emergence years and broods. When a periodicity allele is fixed, only one brood is fixed (Fig. 2a (middle)). In contrast, when periodicity is not fixed, annual emergence is seen with variability in adult numbers, but no mass emergence occurs (Fig. 2b (middle)). We also investigated the genotypic population sizes, including the juveniles (Fig. 2a (bottom) and 2b (bottom)). In the cooler climate, the total population size increases from approximately 10,000 to approximately 15,000 individuals (Fig. 2a (bottom)). Here, almost all individuals are homozygous for the periodical alleles of one brood at the locus determining the timing of emergence. In contrast, in the warmer climate, no periodicity is fixed, not even with the shortest periodicity of 10 years (Fig. 2b). In stochastic models, without an example of a simulation run, it is difficult for readers to imagine how the temporal dynamics looks like. We actually run the simulations several times. The qualitative results are summarized in Figure 3 based on 50 runs. For example, when the periodicity is fixed (Fig. 2a), all fifty runs show fixation (the left column in Fig. 3a), even though the timing of fixation is different among simulations.

We examined the simulation dynamics by varying the introduced periodicity from 10 to 20 years and the ART from +1 to -2 at step=0.1 (Fig. 3). There is a border of extinction such that if the climate is cooler than the threshold, the population usually goes extinct. However, some cicadas survive under such conditions in a small number of runs. If the climate is warmer than this threshold, cicadas survive in almost all simulation runs. Periodicity is fixed at and near the boundary of extinction. A wide band of fixed periodicity is found slightly below the boundary of extinction, where the shorter (longer) cycles are fixed at warmer (cooler) cumulative temperatures. A small band of 10-12 years is also observed at the boundary of extinction (Fig. 3a). As a control, we also ran the simulation without introducing mutations (Fig. 3b). The surviving regions of both experiments and controls largely agree (the extinction region is almost identical in Fig. 3a (right) and 3b (right)). However, under short life cycles, the conditions under which cicadas survive are slightly broader than those of the controls. We also note that some extinction is observed slightly below the complete extinction borders (ART=-0.5 to 0.0). The survival region above this area (ART=-1.0 to -0.5) might be in the extinction zone (green area in Fig. 3), but survival in this region appears to be possible due to a combination of cycles, growth rates and initial conditions.

We also tested various extinction conditions. In the current models, all non-periodical nymphs that cannot mature within the introduced periods are assumed to die. First, we removed the period limitation of longevity for non-periodical cicadas, allowing non-periodical nymphs to survive until 50 years, i.e., the maximum longevity setting. Surprisingly, this removal of the limitation of juvenile longevity greatly relaxed the fixation condition for periodical cicadas (Fig. S3 vs. Fig. 3). When the extinction threshold N_c was lowered from $N_c=300$ to $N_c=100$ and $N_c=0$, the region of periodicity fixation was drastically enlarged (Fig. S4). However, the thresholds of extinction at $N_c=100$ and $N_c=300$ are almost

identical, and the trend of fixation of longer cycles at lower temperatures was similar. We also inspected the case when the Allee effects are variable depending on the adult population size N_A . We found a slight decrease in the area of fixation but no qualitative differences (Fig. S5 vs. Fig. 3). We also tested various parameter k values of annual mortality rate (Fig. S6). Mortality may be affected by yearly temperatures, such that lower temperatures increase nymphal mortality. Freezing temperatures will not only reduce the amount of root water flow available to the nymphs but also promote nymph desiccation, resulting in high nymph mortality. We assume that a cool environment has a low k ($=200$). In contrast, a warm environment has a high k ($=300$). In this case, extinction occurred under conditions of much higher ART, resulting in the extinction of longer cycles (16-20 years). We also assume that a cool environment has a high λ parameter value ($=1.007$). In contrast, a warm environment has a low λ ($=1.003$). Here, we found almost no qualitative changes in the outcomes (Fig. S7).

In our simulation, we assumed that the periodicity allele is dominant, whereas the temperature-dependent allele is recessive (Figs 2 and 3). We also tested the fixation of the periodicity allele when the temperature-dependent allele is dominant (i.e., the periodicity allele is recessive) under a wide range of mutation rates (0.001 to 0.01). Under this condition, the fixation of periodicity is observed when the mutation rate is sufficiently large (Figs. S8, S9). We also found that shorter periods are associated with the fixation of periodicity even at even low mutation rates. We also tested the fixation of recessive periodicity allele when the period limitation of longevity for non-periodical cicadas is removed (Fig S3). The periodicity fixation is observed in a wider range of average relative temperature (e.g., Fig. S10 for 10-year cycle), compared to those with period limitation (Fig. S8a). Thus, the dominant/recessive nature of the periodicity allele quantitatively affects the threshold mutation rates for periodicity evolution, but it does not affect the evolution of periodicity

itself (Figs. S8, S9, S10). The evolution of periodicity should occur over a long run, irrespective of allele dominance, as long as extinction does not occur. Here, we present results based on the condition that an individual cannot have multiple independent mutations. The results are approximately the same with multiple independent mutations (Fig. S11). We also tested discretized and truncated normal distributions with high and low variability (standard deviation=0.5 and 1.0, respectively) that more closely resemble the natural condition of habitat variation. We found no qualitative changes (Fig. S12).

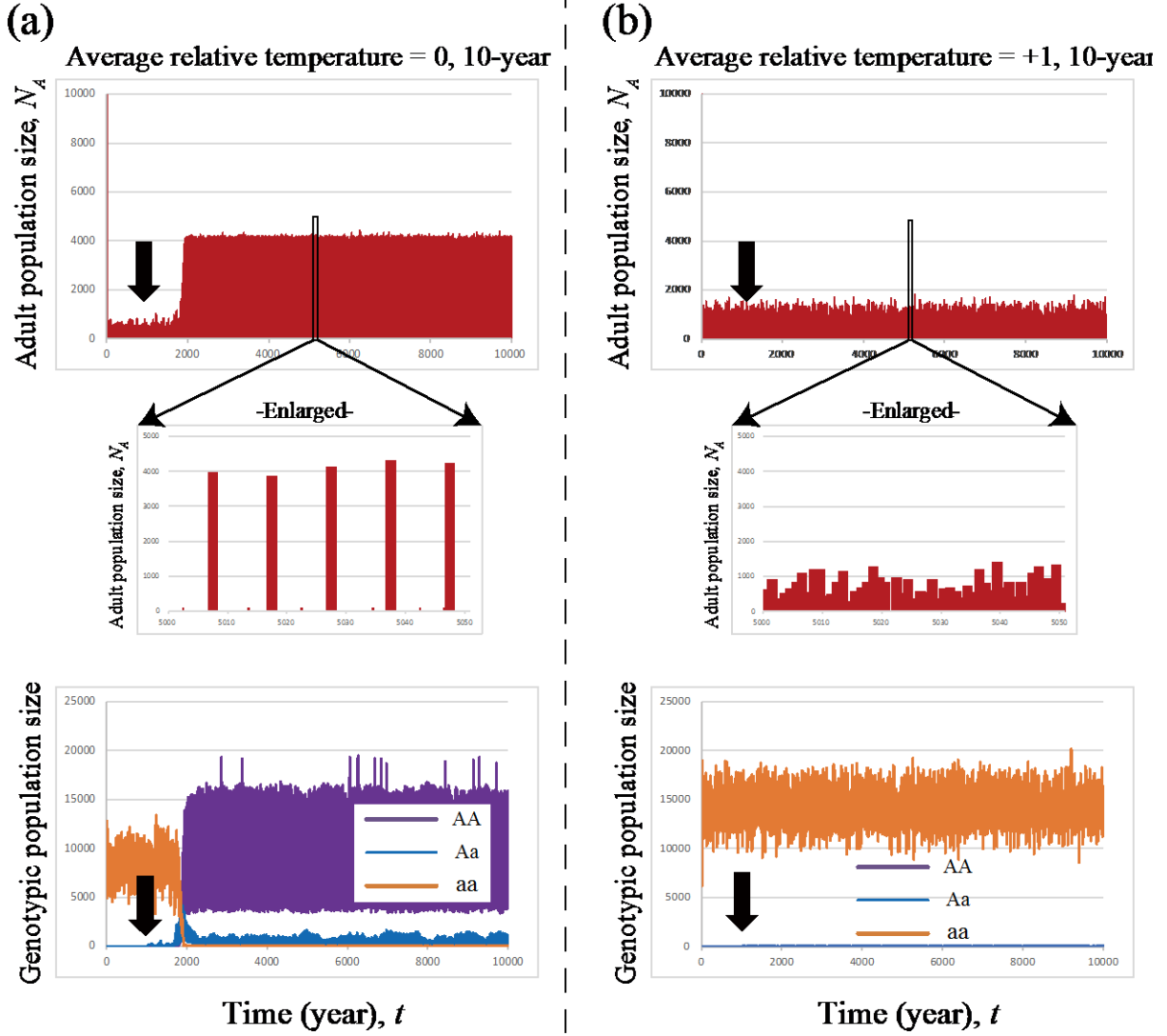


Fig. 2. Temporal dynamics of cicada populations with 10-year periodicity introduced under cool and warm ambient environments. (a) Cool environments (ART=0) and (b) warm environments (ART=+1). (top) Annual adult population sizes. (middle) Enlargement of top for $t=5000\sim5050$. (bottom) Annual total population sizes for each genotype (AA: purple, Aa: blue, aa: orange). The black arrow points to the first step ($t=1,000$) when the mutation is introduced. The extinction threshold of the Allee effect is set as $N_c=100$. The parameters for annual mortality are $k=250$ and $\lambda=1.005$. The penalty of reproduction for immature periodical adults is set to be dependent on the shortage of accumulated temperature.

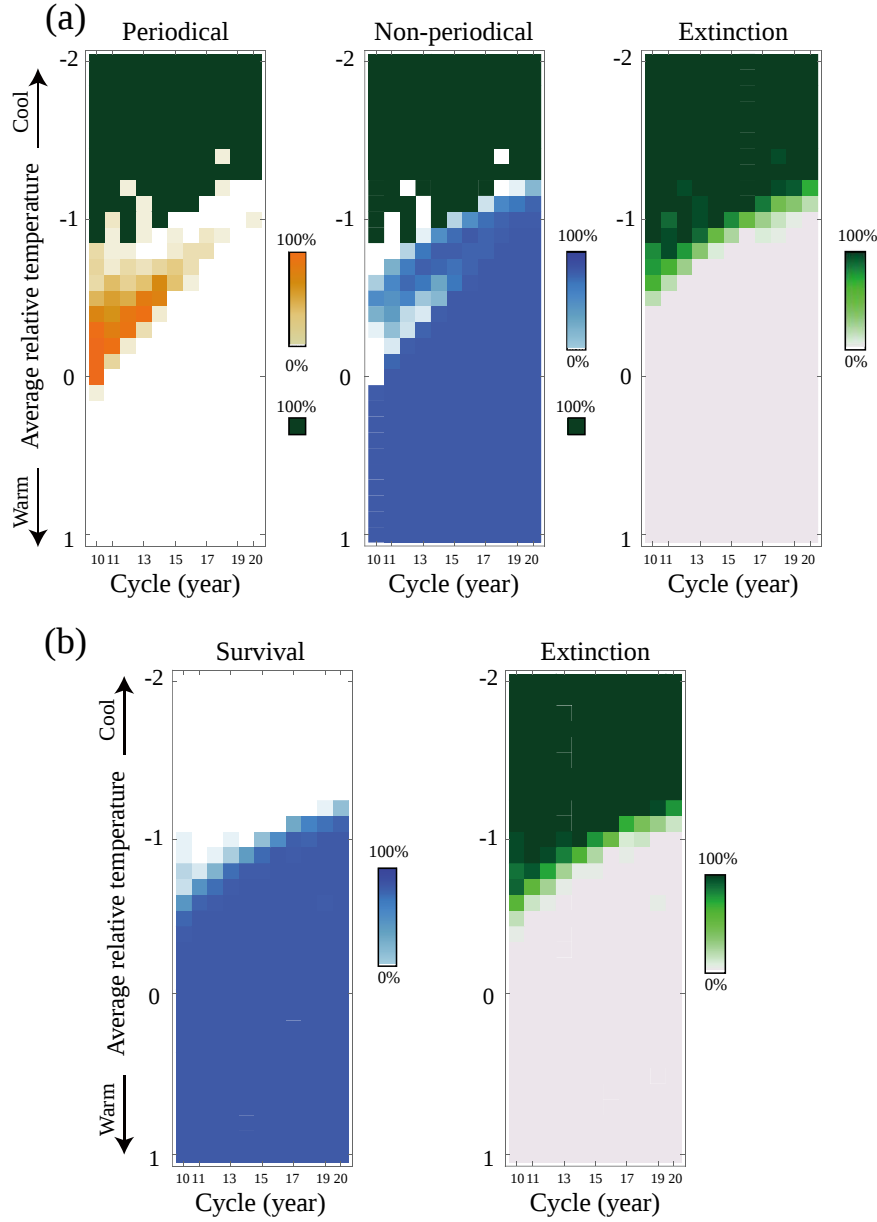


Fig. 3. Phase diagrams of 10- to 20-year periodicity introductions versus average relative temperature (ART). (a) Mutation experiment (left: fixation; middle: no fixation; right: extinction). (b) Control (no mutation) (left: survival; right: extinction). Green areas: extinction; orange: fixation of periodicity; blue: no fixation (darker colours indicate higher probabilities). The extinction threshold of the Allee effect is set as $N_c=100$. The parameters for annual mortality are $k=250$ and $\lambda=1.005$. The penalty of reproduction for immature periodical adults is set to be dependent on the shortage of accumulated temperature. The results are based on 50 simulation runs for each condition.

4. Discussion

Our computer simulation demonstrates that the evolution of periodicity [20] is possible under highly restricted conditions. If our model accurately captures the evolution of periodicity in *Magicicada*, then cooling during glacial periods [27] must have been a critical factor in *Magicicada* evolution and the conditions in glacial refugia must have been similar to those in our model. Surprisingly, longer life cycles are not fixed at the boundary of extinction, probably because population sizes under such conditions are too small to permit the fixation of periodical cycles (Figs. 3a). In shorter cycles, fixation may be achieved at the verge of extinction because the cicadas with a shorter cycle reproduce more frequently (Figs. 3a). When the total time steps are increased from 10,000 to 30,000, the results are almost identical, indicating that 10,000 steps are sufficient to reach a steady state in the current simulation (Fig. S13).

In our model, when switching to periodicity takes place, the periodical cicadas converge to a single brood (Fig. 2a (middle)). In the initial stages of evolution, there may be a few broods (different emergence-year cycles) of periodical mutants; however, only one brood survives and all other founder broods appear to be eliminated by Allee effects and yearly nymphal mortality. All smaller founder broods suffer strong Allee effects, and only the largest of the broods appear to avoid Allee effects and persist. Without Allee effects ($N_c=0$), a few small broods persist alongside one large brood for a while, but they are eventually eliminated by the constant annual nymphal mortality (Fig. S9c vs. Fig. 2a). In contrast, even under weak Allee effects ($N_c \leq 50$), small founder broods are immediately eliminated. The current accumulated data on the distribution of periodical cicadas suggest that broods are largely non-overlapping [28, 29]. Such habitat exclusion, i.e., one location-one brood, may be the result of mechanisms similar to those in our model. We also observe a drastic increase in

adult emergence and maximal nymphal population sizes (Fig. 2a (bottom) and 2b (bottom)). If our model dynamic is realistic, then the extraordinary mass emergence of periodical cicadas may be partly attributed to the processes involved in the evolution and fixation of periodicity.

Under stronger Allee effects (from $N_c=100$ to $N_c=300$), the extinction threshold at which periodicity is acquired is lowered (Fig. S4). This pattern may arise because the rare periodicity mutants in small populations are eliminated by the Allee effects, particularly during the early stages, which sharply reduces the fixation probability of the periodicity allele. In fact, if the Allee effect is weak or non-existent ($N_c=0$), periodicity spreads under a wide range of conditions. Similarly, as a periodical life cycle becomes longer, the probability of periodicity acquisition gradually lowers due to several reasons: First, cicadas with longer life cycles are exposed to cumulative annual mortality more times than are those with shorter life cycles, and the effects of cumulative mortality are reset less often by opportunities for reproduction. Second, the adult emergence tends to spread out in longer cycles because of the unevenness of juvenile growth is increased among individuals. This results in a lower probability of fixation in longer cycles. Above all, there are fewer opportunities for periodicity allele fixation in longer cycles because there is a lower total number of life cycles (generations) per given period. For example, 10-year cicadas reproduce twice in a 20-year period, whereas 20-year cicadas reproduce only once during this time. Cumulative mortality and limited mating opportunities may be one of the primary reasons why 19-year cicadas are not observed in nature.

This simulation model is not a dynamic model with gradual geological cooling; rather, it is a stochastic dynamic model with yearly variation under a range of cold climates. We did not use a dynamic model because the yearly stochastic variation in climates is several magnitudes larger than the geological cooling. By testing a wide range of cold climates, we can evaluate the effects of geological cooling without dynamic geological models. Our model shows that there are two important components of randomness that contribute to the acquisition of periodicity: (1) yearly stochasticity in climate and (2) variations in microhabitats and individual growth (see Fig. S14). The acquisition of periodicity at and near the boundary of extinction suggests that geological cooling should have contributed to the fixation of periodicity in ancestral cicadas with cumulative temperatures.

Our simulation demonstrates the feasibility of the first step of Yoshimura's (1997) hypothesis for the evolution of periodicity during glacial periods. Our results indicate that various year cycles (10-20 year) could have evolved depending on slight differences in accumulated temperatures. The fixation of periodicity is also exhibited at and near the boundary of extinction, as in the case of selection for prime-numbered cycles [21]. Interestingly, the fixation of periodicity is more likely if the Allee effect is non-existent or weak (i.e., $N_c=0$ or 100), whereas the selection of prime-numbered cycles is promoted by a stronger Allee effect [22]. Therefore, an intermediate Allee effect may be necessary for the evolution of prime-numbered cycles in periodical cicadas. The current results also agree with the approximate distribution of the 17-year cicadas, which are north of the 13-year cicadas.

Previous models have not considered the life history characteristics of the ancestral periodical cicadas [4, 19, 20]. Although all known non-periodical cicadas experience

temperature-dependent growth rates and size-dependent maturation, with adult emergence triggered by the threshold of accumulated temperature (T_{mature} in Fig. 1a), the periodical cicadas are the only known cicadas to exhibit time-dependent maturation. The current results suggest that the evolution of periodicity is plausible, but only under restricted conditions near or at the extinction boundary.

Many periodical organisms are known in the world, e.g., cicadas [16-18] and plants [30-32]. *Magicicada* is associated with prime-numbered life cycles. However, well-known bamboo plants are estimated to have 15-, 30-, 60-, and 120-year life cycles, and possibly more, almost all of which are non-prime cycles [30, 32]. Recently, a subtropical plant, *Strobilanthes flexicaulis*, was confirmed to have a 6-year life cycle [31]. Fijian and Indian cicadas exhibiting mass emergence are also suspected to be periodical under shorter life cycles [16-18]. If these cicadas are periodical, their evolutionary mechanism for periodicity should be different from that of the *Magicicada* group. The 17- and 13-year life cycles of the *Magicicada* group are unique among all periodical organisms because of their extremely long, prime-numbered cycles.

Non-periodical maximum virtual longevity (50 years)

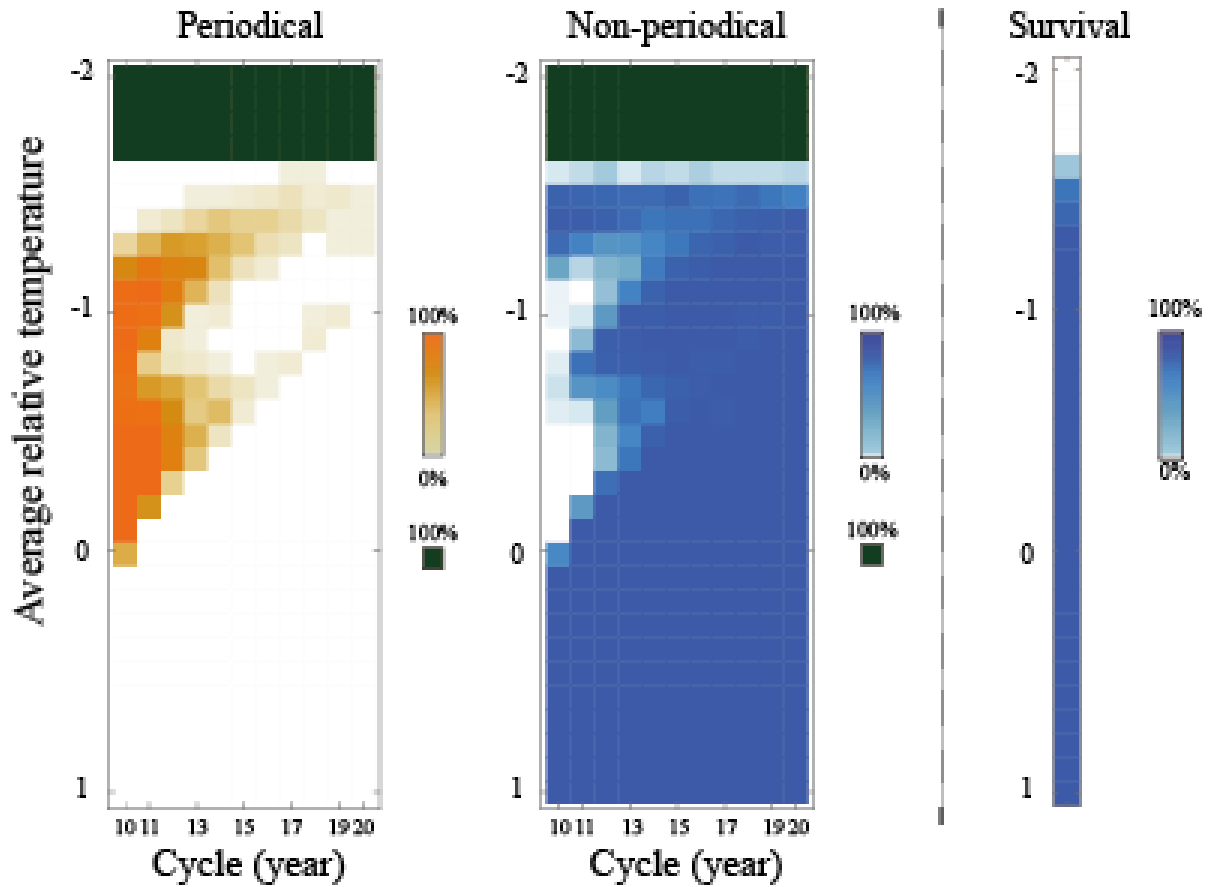


Fig. S3. Phase diagrams of 10- to 20-year periodicity introductions versus average relative temperature (ART) when the longevity of non-periodical cicada nymphs is 50 years. (left, middle) Mutation experiment (left: fixation; middle: no fixation). (right) Control (no mutation introduced, survival). Green areas: extinction; orange: fixation of periodicity; blue: no fixation (darker colours indicate higher probabilities). The results are based on 50 simulation runs for each condition. The Allee effect is set as the critical population size N_c , below which the population is set to extinction, such that $N_c=100$. The annual mortality parameter is set as $k=250$, $\lambda=1.005$. The penalty of reproduction due to immature periodical cicadas is set to be dependent on the shortage of accumulated temperature.

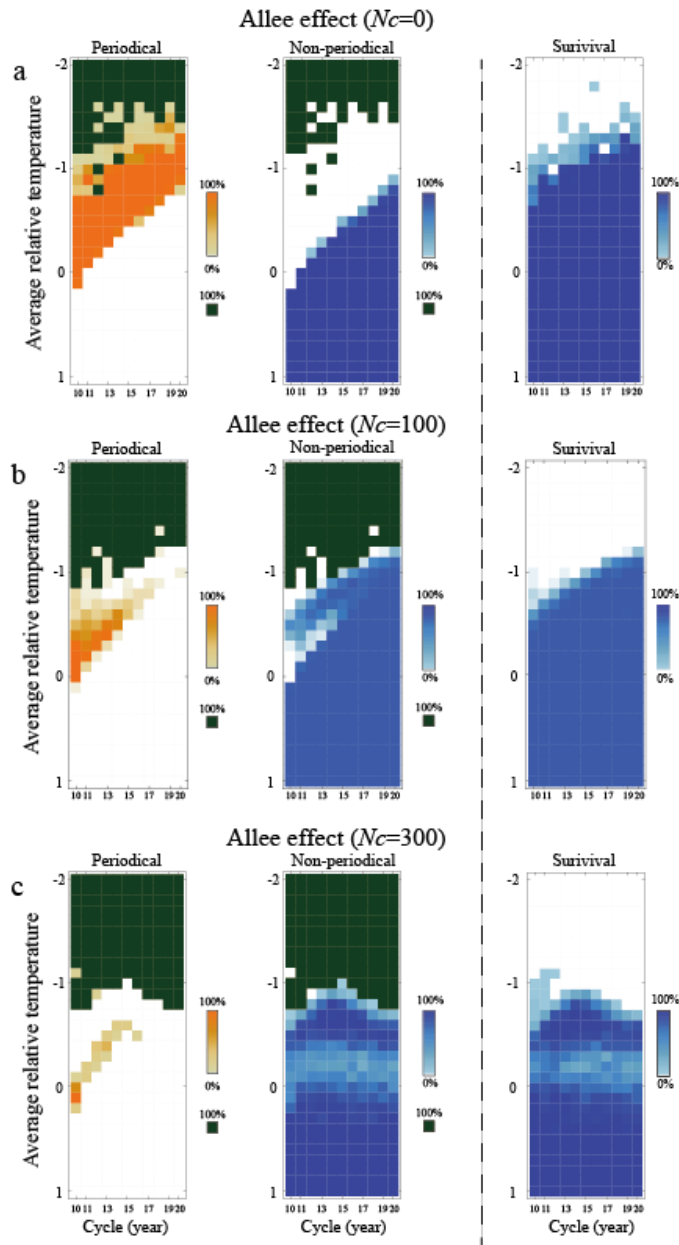


Fig. S4. Phase diagrams of 10- to 20-year periodicity introductions versus average relative temperature (ART) with three different levels of extinction threshold N_c for the Allee effects. (a) $N_c=0$, (b) $N_c=100$, (c) $N_c=300$. (left, middle) Mutation experiment (left: fixation; middle: no fixation). (right) Control (no mutation, survival). Green areas: extinction; orange: fixation of periodicity; blue: no fixation (darker colours indicate higher probabilities). The parameters for annual mortality are $k=250$ and $\lambda=1.005$. The penalty of reproduction due to immature periodical cicadas is set to be dependent on the shortage of accumulated temperature. The results are based on 50 simulation runs for each condition.

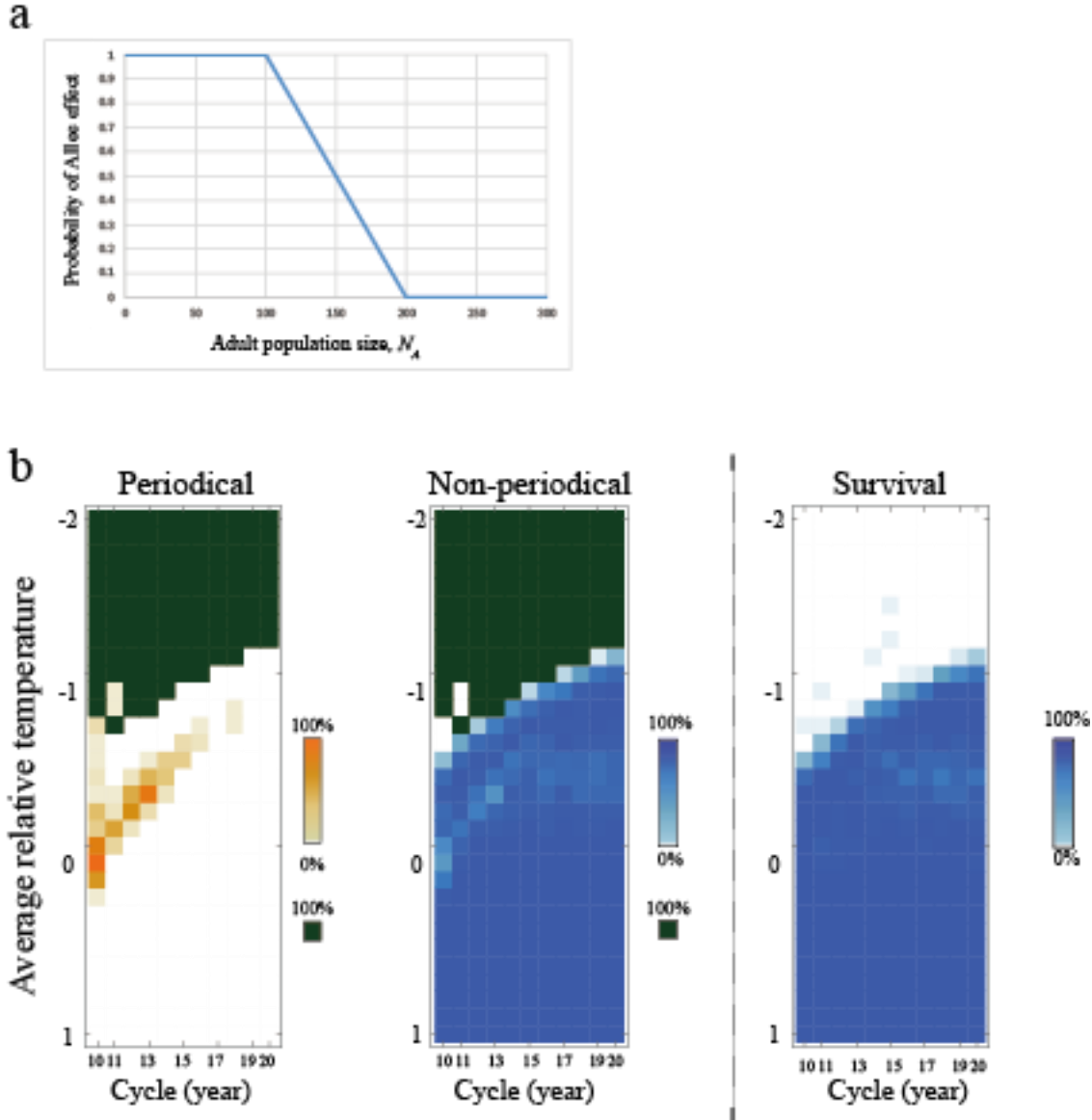


Fig. S5. Phase diagrams of 10- to 20-year periodicity introductions versus average relative temperature (ART) with varying degrees of extinction thresholds N_c for the Allee effects. (a) Probability of the Allee effect (N_c), i.e., $p(N_c=N_A)$. If $N_A < 100$, $p=1$; if $100 \leq N_A \leq 200$, $p = -N_A/100 + 2$; and if $N_A > 200$, $p=0$. (b) (left, middle) Mutation experiment (left: fixation; middle: no fixation). (right) Control (no mutation, survival). Green areas: extinction; orange: fixation of periodicity; blue: no fixation (darker colours indicate higher probabilities). The parameters for annual mortality are $k=250$ and $\lambda=1.005$. The penalty of reproduction due to immature periodical cicadas is set to be dependent on the shortage of accumulated temperature. The results are based on 50 simulation runs for each condition.

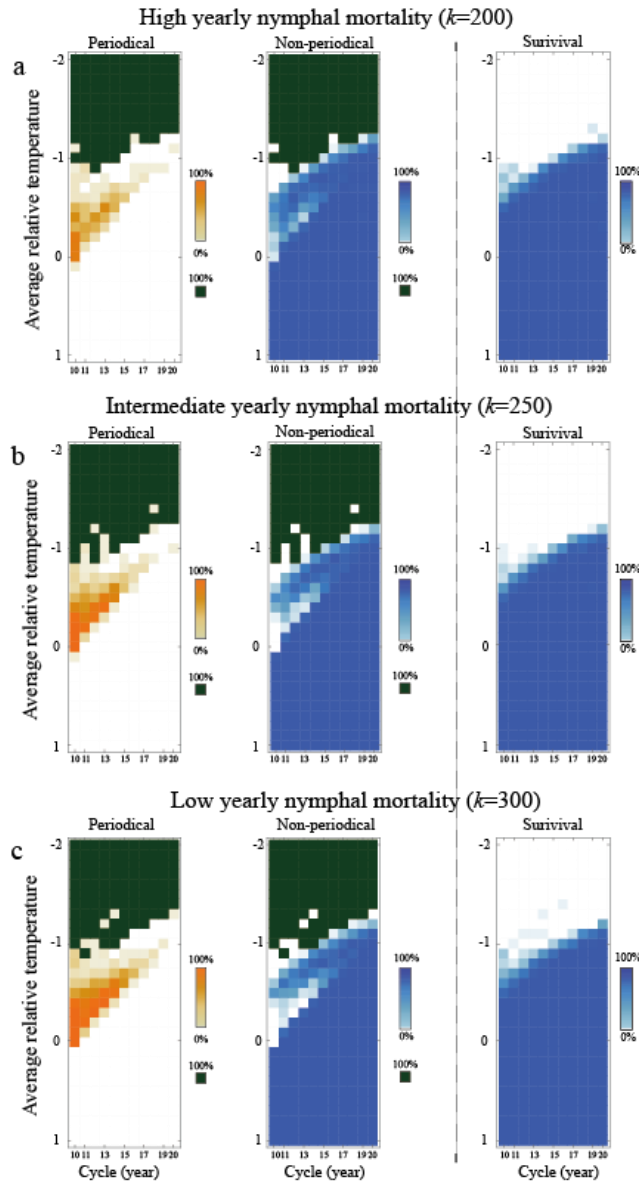


Fig. S6. Phase diagrams of 10- to 20-year periodicity introductions versus average relative temperature (ART) with three different yearly nymph mortality rates.

Parameter k is varied, while parameter λ is held constant ($\lambda=1.005$). (a) $k=200$, (b) $k=250$, (c) $k=300$. (left, middle) Mutation experiment (left: fixation; middle: no fixation). (right) Control (no mutation, survival). Green areas: extinction; orange: fixation of periodicity; blue: no fixation (darker colours indicate higher probabilities). The extinction threshold of the Allee effect is set as $N_c=100$. The penalty of reproduction due to immature periodical cicadas is set to be dependent on the shortage of accumulated temperature. The results are based on 50 simulation runs for each condition.

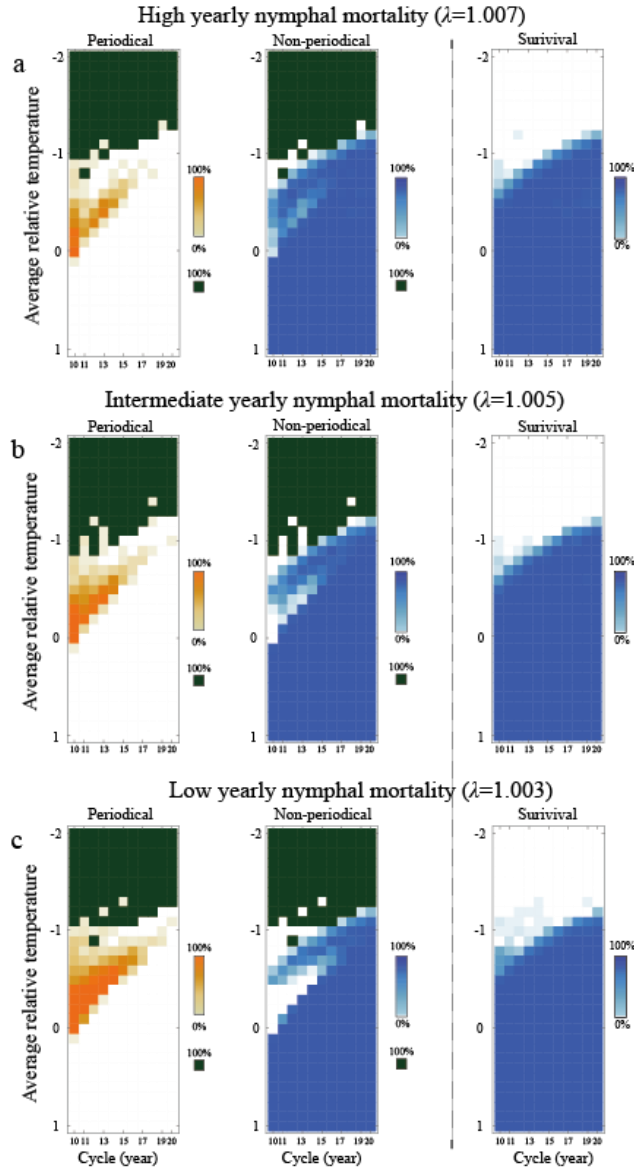


Fig. S7. Phase diagrams of 10- to 20-year periodicity introductions versus average relative temperature (ART) with three different yearly nymph mortality rates.

Parameter λ is varied, while parameter k is held constant ($k = 250$). (a) $\lambda = 1.007$, (b) $\lambda = 1.005$, and (c) $\lambda = 1.003$. (**left, middle**) Mutation experiment (**left**: fixation; **middle**: no fixation). (**right**) Control (no mutation, survival). Green areas: extinction; orange: fixation of periodicity; blue: no fixation (darker colours indicate higher probabilities). The extinction threshold of the Allee effect is set as $N_c = 100$. The penalty of reproduction due to immature periodical cicadas is set to be dependent on the shortage of accumulated temperature. The results are based on 50 simulation runs for each condition.

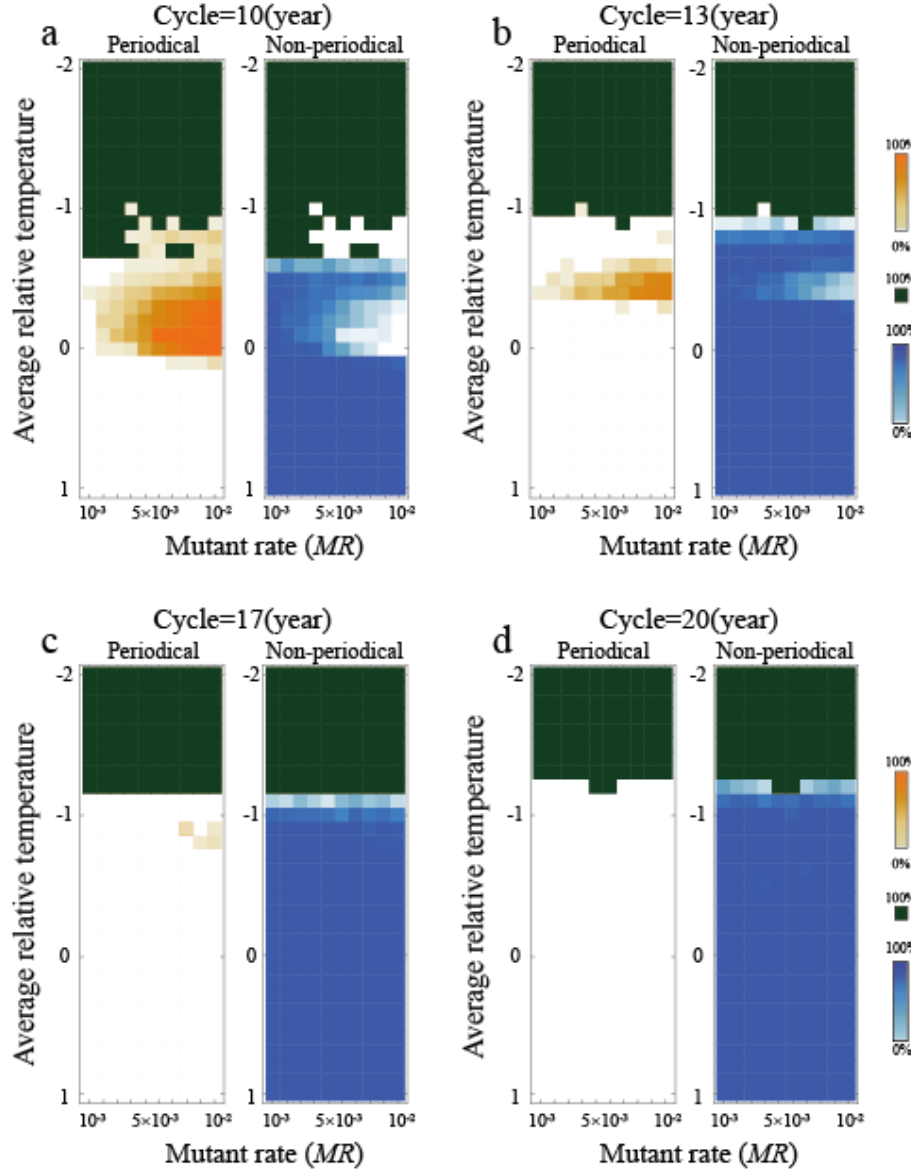


Fig. S8. Phase diagrams of periodicity introduction with varying levels of mutation rates versus average relative temperature (ART) with four different periods when the non-periodical allele is dominant. (a) 10-year period, (b) 13-year period, (c) 17-year period, (d) 20-year period. Mutation rates range from 10^{-3} to 10^{-2} (interval= 10^{-3}). **Left: fixation; **right:** no fixation. Green areas: extinction; orange: fixation of periodicity; blue: no fixation (darker colours indicate higher probabilities). The extinction threshold of the Allee effect is set as $N_c=100$. The parameters for annual mortality are $k=250$ and $\lambda=1.005$. The penalty of reproduction for immature periodical adults is set to be dependent on the shortage of accumulated temperature. The results are based on 50 simulation runs for each condition.**

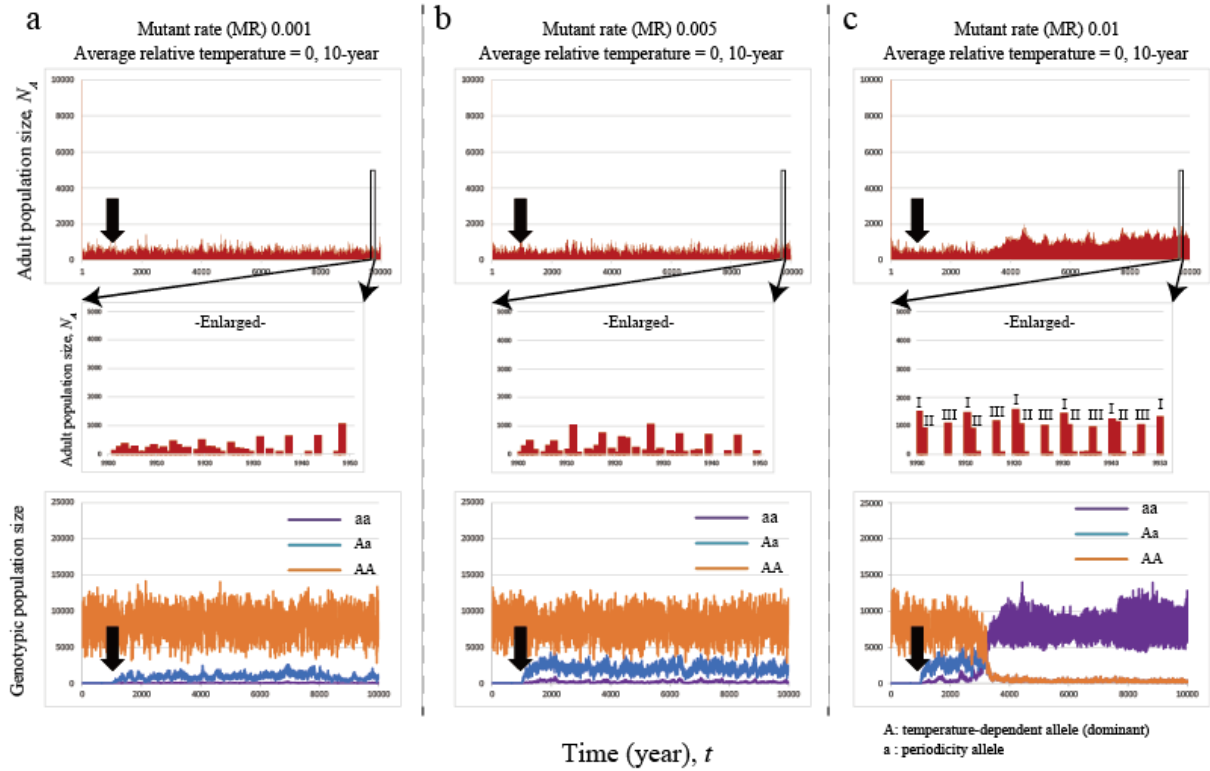


Fig. S9. Temporal dynamics of cicada populations with 10-year periodicity introduced and the non-periodicity allele set as dominant. (a) Mutation rate=0.001, (b) mutation rate=0.005, and (c) mutation rate=0.01. **(top)** Annual adult population sizes. **(middle)** Enlargement of **top** for 9900~9950, including three different broods (Broods I, II, and III). **(bottom)** Annual total population sizes for each genotype (*AA*: purple, *Aa*: blue, *aa*: orange). The black arrow points to the first step ($t=1,000$) when the mutation is introduced. The extinction threshold of the Allee effect is set as $N_c=100$. The parameters for annual mortality are $k=250$ and $\lambda=1.005$. The penalty of reproduction for immature periodical adults is set to be dependent on the shortage of accumulated temperature.

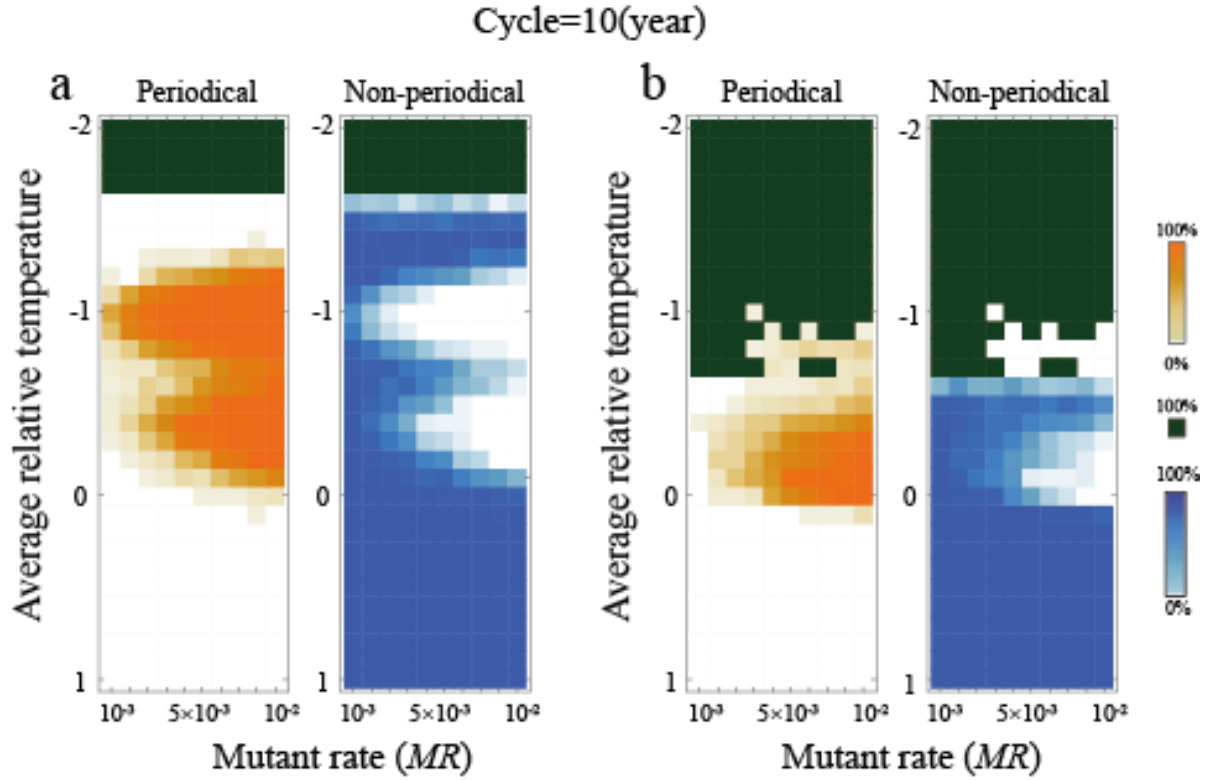


Fig. S10. Phase diagrams of periodicity introduction with varying levels of mutation rates versus average relative temperature (ART) with 10-year period when the non-periodical allele is dominant. (a) The longevity of non-periodical cicada nymphs is 50 years, (b) non-periodical cicadas automatically die if they do not mature within a set period (same as Fig. S8a). Mutation rates range from 10^{-3} to 10^{-2} (interval= 10^{-3}). **Left:** fixation; **right:** no fixation. Green areas: extinction; orange: fixation of periodicity; blue: no fixation (darker colours indicate higher probabilities). The extinction threshold of the Allee effect is set as $N_c=100$. The parameters for annual mortality are $k=250$ and $\lambda=1.005$. The penalty of reproduction for immature periodical adults is set to be dependent on the shortage of accumulated temperature. The results are based on 50 simulation runs for each condition.

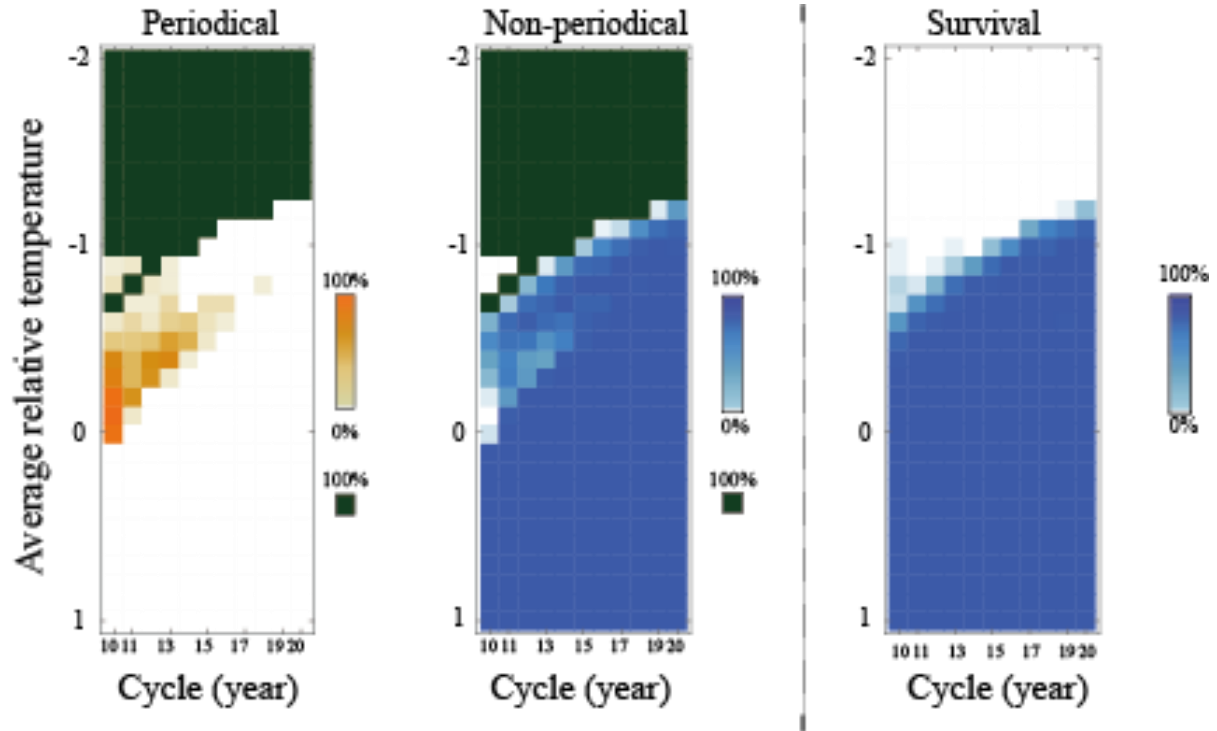


Fig. S11. Phase diagrams of 10- to 20-year periodicity introductions versus average relative temperature (ART) when a single allelic mutation is allowed for an individual. (left, middle) Mutation experiment (left: fixation; middle: no fixation). (right) Control (no mutation, survival). Green areas: extinction; orange: fixation of periodicity; blue: no fixation (darker colours indicate higher probabilities). The extinction threshold of the Allee effect is set as $N_c=100$. The parameters for annual mortality are $k=250$ and $\lambda=1.005$. The penalty of reproduction due to immature periodical cicadas is set to be dependent on the shortage of accumulated temperature. The results are based on 50 simulation runs for each condition. See text for details.

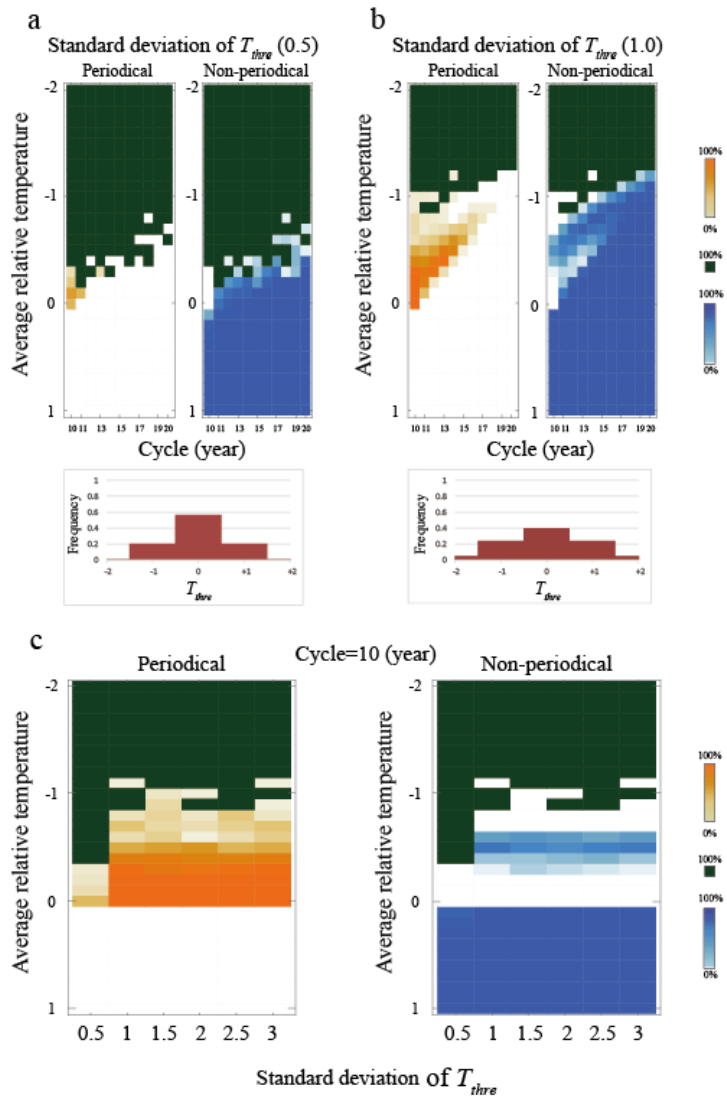


Fig. S12. (a, b) Phase diagrams of 10- to 20-year periodicity introductions versus average relative temperature (ART) with variability in microhabitats. Microhabitat variation follow a discretized and truncated normal distribution. **(a)** Low variability (standard deviation=0.5) and **(b)** high variability (standard deviation=1.0). **(c)** Varying variability (standard deviation=0.5-3.0). **(left: fixation; right: no fixation).** Green areas: extinction; orange: fixation of periodicity; blue: no fixation (darker colours indicate higher probabilities). The Allee effect is set as $N_c=100$. The parameters for annual mortality are $k=250$ and $\lambda=1.005$. The penalty of reproduction for immature periodical adults is set to be dependent on the shortage of accumulated temperature. The results are based on 50 simulation runs for each condition.

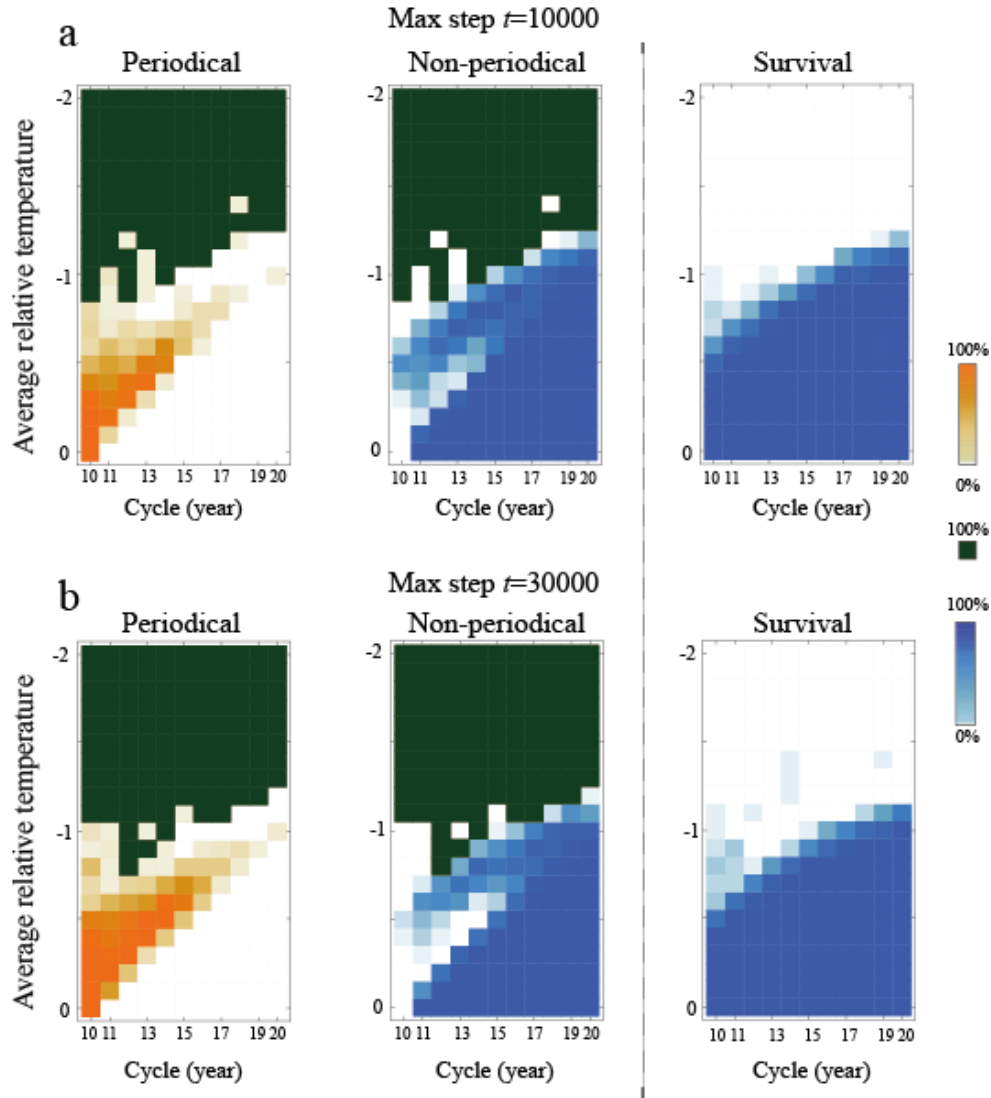


Fig. S13. Phase diagrams of 10- to 20-year periodicity introductions versus average relative temperature (ART) with two different final time steps. (a) Final $t=10,000$, and (b) final $t=30,000$. (left, middle) Mutation experiment (left: fixation; middle: no fixation). (right) Control (no mutation, survival). Green areas: extinction; orange: fixation of periodicity; blue: no fixation (darker colours indicate higher probabilities). The extinction threshold of the Allee effect is set as $N_c=100$. The parameters for annual mortality are $k=250$ and $\lambda=1.005$. The penalty of reproduction for immature periodical adults is set to be dependent on the shortage of accumulated temperature. The results are based on 50 simulation runs for each condition. ART is varied from -2 to 0 because the simulation time is exceedingly elongated if $ART>0$.

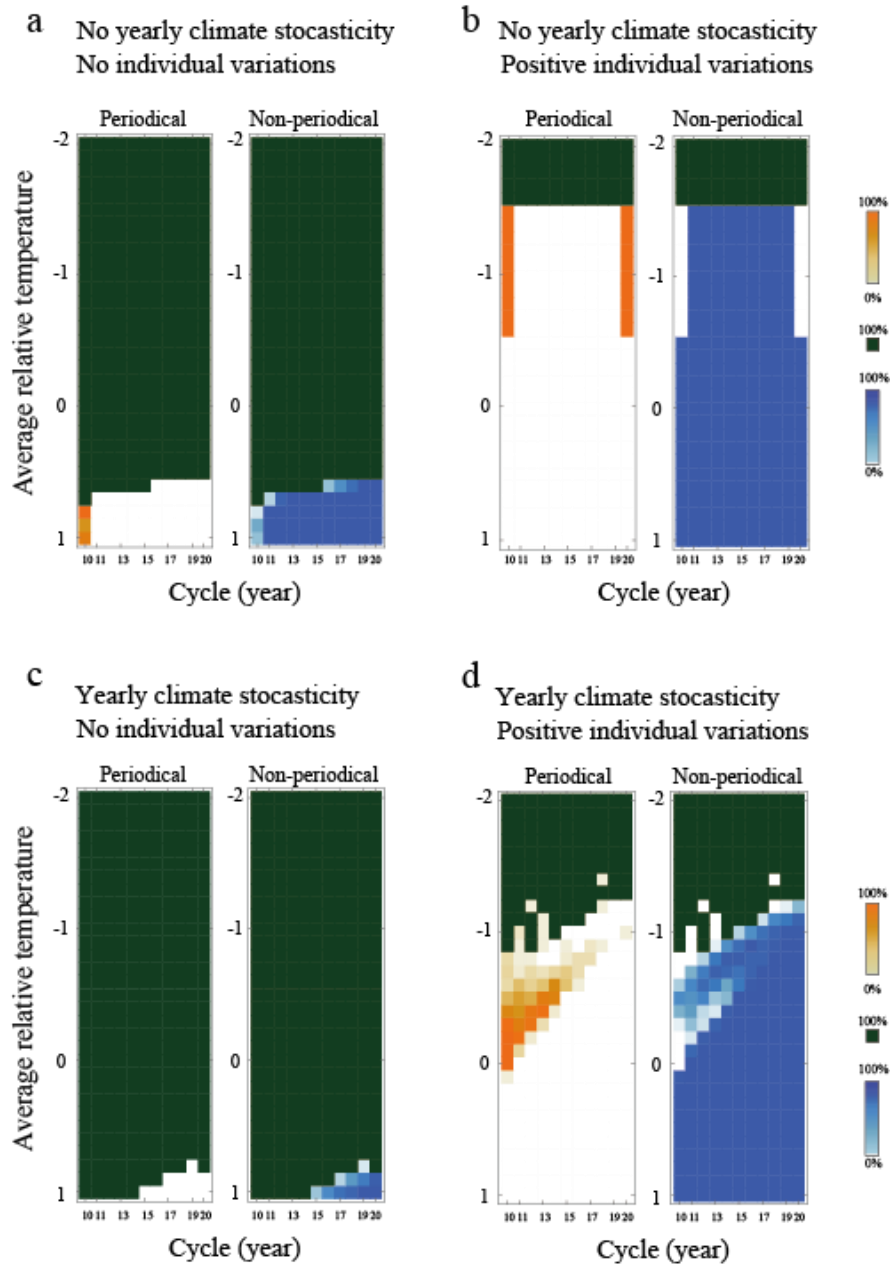


Fig. S14. Phase diagrams of 10- to 20-year periodicity introductions versus average relative temperature (ART) with/without yearly climate stochasticity and individual microhabitat variations. (a) No climate stochasticity and no individual variations, (b) no climate stochasticity but positive individual variations, (c) positive climate stochasticity but no individual variations, and (d) positive climate stochasticity and positive individual variations (same as Fig. 3). (left) Fixation, (right) no fixation. Green areas: extinction; orange: fixation of periodicity; blue: no fixation (darker colours indicate higher probabilities).

The extinction threshold of the Allee effect is set as $N_c=100$. The parameters for annual mortality are $k=250$ and $\lambda=1.005$. The penalty of reproduction for immature periodical adults is set to be dependent on the shortage of accumulated temperature. The results are based on 50 simulation runs for each condition. Note that cycles (periods) correspond with the climatic conditions that evolve with periodicity when there is no yearly climate stochasticity, e.g., during the 10-year period in **(a)** and **(b)**. Without individual microhabitat variations (**a** and **c**), the extinction boundary is greatly extended towards the warm climate because all individuals are very similar.

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Table 1. List of Parameters.

Term	Unit	Explanation
t	Year	Time step (year)
T	°C	Yearly ambient temperature (random)
T_{mean}	°C	Average of yearly ambient temperature
τ	Year	Cycle (period) length
T_{thre}	°C	Lower yearly temperature limit for positive growth
$T_{thre-average}$	°C	Average of yearly temperature threshold is set to 19 and the variability is $T_{thre-average} \pm 2$ with equal probabilities
T_{accume}	°C	Sum of yearly accumulated temperature
T_{mature}	°C	Amount of the accumulated temperature required for maturation (adult emergence)
ART	$\Delta^{\circ}\text{C}$	Average relative temperature= $(T_{mean}-T_{thre-average})$
N_c	No. individuals	Extinction threshold for adult populations set by the Allee effect
N_n	No. nymphs	Population size of nymphal cicadas
N_A	No. Adults	Population size of adult cicadas
b	No. eggs/ Adult	Birth rate is set as $b=10$
$b_{p,suff}$	No. eggs/ Adult	Birth rate of a periodical adult female with sufficient accumulated temperature ($T_{accume}(\tau) \geq T_{mature}=10$)
$b_{p,ins}$	No. eggs/ Adult	Birth rate of a periodical adult female with insufficient accumulated temperature ($T_{accume}(\tau) < T_{mature}=10$)
$DR(t)$	Probability	Mortality rate at time t (probability)
k		Parameter of yearly nymphal mortality ($DR(t)$)
λ		Parameter of yearly nymphal mortality ($DR(t)$)

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