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メタデータ	言語: en				
	出版者: American Chemical Society				
	公開日: 2018-02-13				
	キーワード (Ja):				
	キーワード (En):				
	作成者: Oka, Toshihiko, Saiki, Takahiro, Alam, Jahang				
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URL	http://hdl.handle.net/10297/00024649				

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# Activation Energy of the Low-pH-Induced Lamellar to Bicontinuous Cubic Phase Transition in Dioleoylphosphatidylserine/Monoolein

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**Supporting Information** 

**ABSTRACT:** Electrostatic interaction is an important factor for phase transitions between lamellar liquid-crystalline  $(L_{\alpha})$  and inverse bicontinuous cubic  $(Q_{II})$  phases. We investigated the effect of temperature on the low-pH-induced  $L_{\alpha}$  to double-diamond cubic  $(Q_{II}^{D})$  phase transition in dioleoylphosphatidyl-serine (DOPS)/monoolein (MO) using time-resolved small-angle X-ray scattering with a stopped-flow apparatus. Under all conditions of temperature and pH, the  $L_{\alpha}$  phase was directly



transformed into an intermediate inverse hexagonal  $(H_{II})$  phase, and subsequently the  $H_{II}$  phase slowly converted to the  $Q_{II}^{D}$  phase. We obtained the rate constants of the initial step (i.e., the  $L_{\alpha}$  to  $H_{II}$  phase transition) and of the second step (i.e., the  $H_{II}$  to  $Q_{II}^{D}$  phase transition) using the non-negative matrix factorization method. The rate constant of the initial step increased with temperature. By analyzing this result, we obtained the values of its apparent activation energy,  $E_a$  ( $L_{\alpha} \rightarrow H_{II}$ ), which did not change with temperature but increased with an increase in pH. In contrast, the rate constant of the second step decreased with temperature at pH 2.6, although it increased with temperature at pH 2.7 and 2.8. These results indicate that the value of  $E_a$  ( $H_{II} \rightarrow Q_{II}^{D}$ ) at pH 2.6 increased with temperature, but the values of  $E_a$  ( $H_{II} \rightarrow Q_{II}^{D}$ ) at pH 2.7 and 2.8 were constant with temperature. The values of  $E_a$  ( $H_{II} \rightarrow Q_{II}^{D}$ ) were smaller than those of  $E_a$  ( $L_{\alpha} \rightarrow H_{II}$ ) at the same pH. We analyzed these results using a modified quantitative theory on the activation energy of phase transitions of lipid membranes proposed initially by Squires et al. (Squires, A. M.; Conn, C. E.; Seddon, J. M.; Templer, R. H. *Soft Matter* 2009, *5*, 4773). On the basis of these results, we discuss the mechanism of this phase transition.

# 1. INTRODUCTION

Most biomembranes/lipid membranes adopt a lamellar liquidcrystalline  $(L_{\alpha})$  phase, but under certain conditions they form inverse bicontinuous cubic  $(Q_{II})$  phases (e.g., the double-diamond  $Q_{II}^{D}$  (or  $Q^{224}$ ), the primitive  $Q_{II}^{P}$  (or  $Q^{229}$ ), and the gyroid  $Q_{II}^{G}$  (or  $Q^{230}$ ) phases), where the membranes are connected in 3D space with cubic symmetry.<sup>1-5</sup> In the Q<sub>II</sub> phase, an infinite periodic minimal surface (IPMS) lies at the bilayer midplane, which is the interface of two monolayers, and the structures of the Q<sub>II</sub> phases consist of two interwoven networks of water channels, separated by the bilayers.<sup>1</sup> Recently it has been well established that electrostatic interactions due to surface charges of lipid membranes (EI) play various important roles in the structures and phase stabilities of the Q<sub>II</sub> phase. The electrostatic interactions greatly increases the lattice constants and the size of the water channels of the  $Q_{II}\xspace$  phase.  $^{6-10}\xspace$  This may be useful for the crystallization of proteins and the application of biosensors. The modulation of EI induces transitions between the  $L_{\alpha}$  and the  $Q_{II}$  phases and phase transitions between different  $Q_{II}$  phases in various lip-ids.<sup>6,7,11-27</sup> Among these phase transitions, pH-induced phase transitions between the Q<sub>II</sub> phases and the inverse hexagonal  $(H_{II})\ phase^{6,17,21,27}$  and those between the  $L_{\alpha}$  phase and the  $Q_{II}^{D}$  phase<sup>17</sup> have attracted wide attention because the pH is known to control the function and structure of membranes and

proteins, thus playing an indispensable role in cells. We found that the low-pH-induced an  $L_{\alpha}$  to  $Q_{II}^{D}$  phase transition in dioleoylphosphatidylserine (DOPS)/monoolein (MO) membranes and that this phase transition was reversible.<sup>17</sup> Low pH decreases the surface charge density of the DOPS/MO membranes by protonation of the carboxylic acid of DOPS, and as a result the decrease in the electrostatic interactions induces the  $L_{\alpha}$  to  $Q_{II}^{D}$  phase transition. (See ref 17 for the detailed mechanism.) DOPS and MO are essential biological lipids, and hence we consider that this phase transition has an important physiological meaning. Moreover, this phase transition is one of the best systems for investigating the kinetic pathway of the EI-induced  $L_{\alpha}/Q_{II}$  phase transitions because H<sup>+</sup> can rapidly enter the MLVs.<sup>28</sup>

To reveal the mechanism behind the  $L_{\alpha}/Q_{II}$  phase transitions, it is important to elucidate the kinetic pathway. In our previous papers, we investigated the low-pH-induced  $L_{\alpha}$  to  $Q_{II}^{\ \ D}$  phase transition in DOPS/MO using time-resolved small-angle X-ray scattering (TR-SAXS).<sup>28,29</sup> In the initial step, the  $L_{\alpha}$  phase was directly transformed to the  $H_{II}$  phase; subsequently, the  $H_{II}$  phase slowly converted to the  $Q_{II}^{\ \ D}$  phase. We obtained

Received:October 10, 2015Revised:January 6, 2016Published:January 14, 2016

the rate constants of the initial step and of the second step. The appearance of this intermediate state (i.e., the metastable  $H_{II}$  phase) was unexpected because this sequence  $(L_{\alpha} \rightarrow H_{II} \rightarrow Q_{II}^{D})$  is different from the phase sequence at equilibrium due to the curvature energy (i.e., the phase appears in order of  $L_{\alpha} \rightarrow Q_{II}^{D} \rightarrow H_{II}$ ).<sup>28</sup> In the temperature–water content phase diagram, a  $Q_{II}$  phase appears between the  $L_{\alpha}$  and the  $H_{II}$  phases during temperature increases or during water content decreases.<sup>1,30–34</sup> We interpreted that this unusual phenomenon occurs as a kinetic trap as a result of the difference in the activation energy; if the activation energy of the rate-determining step in one kinetic pathway (i.e., the  $L_{\alpha}$  to  $Q_{II}^{D}$  phase transition) is much greater than that in the other kinetic pathway (i.e., the  $L_{\alpha}$  to  $H_{II}$  phase first transforms to the  $H_{II}$  phase and then converts to the  $Q_{II}^{D}$  phase.<sup>28,29</sup>

Generally, the activation energy of structural changes can provide us valuable information on their elementary processes and mechanisms. In this study, to get information on the activation energies of two elementary steps of the low-pHinduced  $L_{\alpha}$  to  $Q_{II}^{D}$  phase transition in 20%-DOPS/80%-MO, we investigated the temperature dependence of this phase transition using TR-SAXS. Using a stopped-flow apparatus, a suspension of multilamellar vesicles (MLVs) of 20%-DOPS/ 80%-MO membrane at neutral pH was rapidly mixed with a low-pH buffer at various temperatures, and then the structural change of the membranes in the resultant suspension was observed as a function of time (i.e., pH-jump experiment). By analyzing these results, the rate constants of two elementary steps (i.e., the initial step (the  $L_{\alpha}$  to  $H_{II}$  phase transition) and the second step (the  $H_{II}$  to  $Q_{II}^{D}$  phase transition)) were obtained at various temperatures. On the basis of these data, we succeeded in obtaining the values and the information on the activation energies of two elementary steps. To our knowledge, these are the first values of the activation energies of the  $L_{\alpha}$  to  $H_{II}$  phase transition and the  $H_{II}$  to  $Q_{II}^{D}$  phase transition of lipid membranes. We analyzed these results using quantitative theory on the activation energy of phase transitions of lipid membranes proposed by Squires et al.<sup>35</sup> On the basis of these results, we discuss the mechanism of this phase transition.

#### 2. MATERIALS AND METHODS

MO was purchased from Sigma Chemical Co. (St. Louis, MO, USA). DOPS was purchased from Avanti Polar Lipids (Alabaster, AL, USA). To prepare DOPS/MO-MLVs, 100  $\mu$ L of 10 mM ammonium acetate buffer (pH 6.7) containing 100 mM NaCl (buffer A) was added to the dry DOPS/MO lipid film (10  $\mu$ mol),<sup>28</sup> and then the suspension was mixed several times using a vortex mixer for about 20 s at room temperature (~25 °C). To purify the MLVs, the MLV suspension was centrifuged at 13 000g for 20 min at 25 °C, and then the pellet was resuspended gently in new buffer A without using the vortex mixer.<sup>28</sup> We used this suspension as the purified MLV suspension. The purified MLVs were used within 12 h after preparation. The lipid concentrations of the suspensions were determined by the Bartlett method.<sup>36</sup>

Data of temperature scanning SAXS were obtained at the BL-6A beamline of the Photon Factory in KEK (Tsukuba, Japan). The X-ray wavelength was 0.1500 nm, and the sample-detector distance was 1023 mm. Data were collected using a 2D pixel array detector (PILATUS3 1M, Dectris, Baden, Switzerland). A handmade capillary holder with a Peltier device (9504/125/060B, Ferrotec Co., Tokyo, Japan) was used to obtain temperature scan data. The temperature of the holder was controlled with a Peltier controller (TDC-5000A, Cell System Co., Yokohama, Japan) and was measured with a platinum resistance temperature sensor (Pt100), which was connected to the

Peltier controller. Immediately after the purified DOPS/MO-MLV suspension in buffer A was mixed with 20 mM citrate buffer at various pH values containing 100 mM NaCl (buffer C) in a volume ratio of 1:9 in an Eppendorf tube, the resultant suspension was transferred to a quartz capillary tube with a diameter of 1.0 mm and a thickness of 0.01 mm (Hilgenberg GmbH, Malsfeld, Germany), and the ends of the tubes were sealed with silicone grease. This sample in the capillary was incubated for more than 5 h at room temperature ( $\sim 20$  °C) before the SAXS measurement. After 10 min of incubation of the sample in the capillary in the holder at 20 °C, the temperature of the sample was increased from 20 to 50 °C at a rate of 1 or 0.5 °C/min. During the temperature scan, the SAXS patterns were measured with a timeresolution of 5 s. Lattice constants were determined by fitting two Gauss functions to the (110) and (111) peaks of the Q<sub>II</sub><sup>D</sup> phase and one to the (10) peak of the  $H_{II}$  phase. Peaks at higher angles were excluded from the fitting because their peak intensities were low. The positions of the peaks at higher angles were used in the phase determination of the samples.

We used the same method of TR-SAXS in our previous paper<sup>28</sup> to monitor structural changes in DOPS/MO membranes after a pH jump. TR-SAXS data were obtained at the BL40B2 beamline at SPring-8 (Sayo, Japan). The X-ray wavelength used was 0.1000 nm, and the sample-detector distance was 1150 mm. Data were collected using a 2D pixel array detector (PILATUS 100 K, Dectris, Baden, Switzerland). A stopped-flow apparatus (SFM-CD10, Unisoku, Osaka, Japan) was used to mix rapidly the purified DOPS/MO-MLV suspension in buffer A with 20 mM citrate buffer at various pH values containing 100 mM NaCl (buffer C) in a volume ratio of 1:9. We arranged the stopped-flow apparatus transversely, and thereby the capillary cell was positioned horizontally. The temperature of the apparatus was kept at various values with a water bath circulator (RTE111, Thermo Neslab, NH, USA). After the incubation of the samples (i.e., the MLV suspension and the low-pH buffer) in the stopped-flow apparatus at a specific temperature for 15 min, TR-SAXS measurements were started after 50 ms from a start signal of the stopped-flow apparatus. The mixing dead time of the stopped-flow apparatus was less than 10 ms. The SAXS patterns were recorded for the first 90 s with a resolution of 0.2 s and then for 9 s at various intervals to be equal intervals on a logarithmic time scale of up to 3629 s from the mixing time. The stopped-flow apparatus was moved during X-ray exposure to avoid damage to the sample caused by the X-ray irradiation. After one TR-SAXS measurement of a sample at low pH, we washed the capillary in the stopped-flow apparatus by running the same buffer, distilled water, ethanol, and distilled water several times, and then we measured the SAXS pattern of the capillary containing a buffer to confirm that no membranes were adsorbed in the capillary cell.

The lattice constant, *a*, of the  $Q_{II}^{D}$  phase is determined by  $S = (1/a)\sqrt{h^2 + k^2 + l^2}$ , and that of the  $H_{II}$  phase, which equals the center-to-center distance of adjacent cylinders in the  $H_{II}$  phase, is determined by  $S = (2/\sqrt{3} a)\sqrt{h^2 + k^2 + hk}$ , where *S* is the reciprocal spacing and *h*, *k*, and *l* are Miller indices. A series of sequential 2D ring diffraction patterns were averaged circularly to reduce them to a set of sequential 1D patterns. These patterns were corrected by subtracting the background scatter caused by the capillary and the buffer. The sequential 1D diffraction patterns are equivalent to matrix X(S, t) in which matrix element  $X_{ij}$  corresponds to the intensity at the *i*th scattering vector  $S_i$  and *j*th delay time  $t_j$ .  $m \times n$  matrix X is the product of the  $m \times k$  matrix of the pure component diffraction profiles A and the  $n \times k$  matrix of the concentration time courses *B*, where *k* is the number of components

 $X = AB^{\mathrm{T}} + E$ 

where superscript T denotes the transpose of the matrix. E is the residual matrix containing the data variance or statistical noise which is not explained by  $AB^{T}$ . To analyze matrix X, we applied a non-negative matrix factorization (NMF) method based on a modified alternating least-squares (MALS) algorithm.<sup>37,38</sup> In a typical MALS algorithm, optimized values of A and B are calculated from a random matrix

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alternatingly with the constraint that the values in *A* and *B* are nonnegative. Given fluctuations in the data, we adopted two constraints as follows: (1) the mean values of the adjacent points are non-negative for matrix *A* or larger than  $-1\sigma$  for matrix *B*; (2) the mean value of the first points in matrix *B* without a first component is within  $\pm 1\sigma$ . Parameter  $\sigma$  is the standard deviation of data in the corresponding region. The program was coded on GNU Octave. We used a *k* value of 3, which is the number of components we could distinguish from the contour maps. Data up to 3629 s were used in the calculations. We repeated independent MALS calculations more than 10 times. Converged matrices *A* from the independent calculations were almost identical; this was also true for the *B* matrices.

# 3. RESULTS

3.1. Temperature-pH Phase Diagram of 20%-DOPS/ 80%-MO. First we investigated the temperature-induced phase transitions of 20%-DOPS/80%-MO (molar ratio) membranes at various pH values from pH 2.6 to 2.8. The contour plot shows the SAXS patterns of 20%-DOPS/80%-MO membranes at pH 2.7 recorded during a temperature scan from 20 to 50 °C at a rate of 1 °C/min (Figure 1a). A waterfall plot of the same data is shown in Figure S1 in Supporting Information (SI). At 20 °C, the SAXS peaks which have a spacing ratio of  $\sqrt{2}:\sqrt{3}:\sqrt{4}:\sqrt{6}:\sqrt{8}:\sqrt{9}$  were indexed as the (110), (111), (200), (211), (220), and (221) peaks of a Q<sub>II</sub><sup>D</sup> phase (Figure 1b).<sup>6</sup> At 35 °C, a new weak peak appeared at around S = 0.170nm<sup>-1</sup>, and its intensity increased with time. The SAXS pattern at 50 °C shows the SAXS peaks which have a spacing ratio of  $1:\sqrt{3:2}$ , corresponding to the H<sub>II</sub> phase, indicating that the peak at  $S = 0.179 \text{ nm}^{-1}$  was due to the (10) peak of the H<sub>II</sub> phase. Thereby this result indicates that a  $Q_{II}^{\ D}$  to  $H_{II}$  phase transition started to occur at 35 °C. At 50 °C, the peak intensity of the H<sub>II</sub> phase became strong, but weak, broad peaks probably due to the distorted  $Q_{II}^{D}$  remained around S = 0.13 - 0.15 nm<sup>-1</sup>. At final pH 2.6, we obtained a similar result (Figure S2). Although the peak positions of the (200) peak of the  $Q_{II}^{D}$ phase and the (10) peak of the H<sub>II</sub> phase were similar, on the basis of the other peaks of the  $H_{II}$  phase and the intensity of the (110) and (111) peaks of the  $Q_{II}^{\ D}$  phase, we can judge that a  $Q_{II}^{D}$  to  $H_{II}$  phase transition started to occur at 35 °C.

Figure 1c shows the temperature dependence of the lattice constants of the  $H_{II}$  and  $Q_{II}^{\ D}$  phases. The lattice constant of the  $Q_{II}^{\ D}$  phase was almost constant at lower temperature, but at above 31 °C it decreased with temperature. On the other hand, the lattice constant of the  $H_{II}$  phase decreased from 6.8 nm with an increase in temperature. This result agrees with the temperature dependence of the lattice constant of the  $H_{II}$  phase in other lipid membranes.<sup>32,39</sup> We obtained similar results for the temperature scan from 20 to 50 °C at a rate of 0.5 °C/min.

On the basis of these SAXS experiments, we made the temperature–pH phase diagram (Figure 1d) after the correction of the pH of the solution using data on the temperature dependence of the pH value (Figure S3). The phase transition from the  $Q_{II}^{D}$  to the  $H_{II}$  phase occurred as temperature increased, which agrees with other researches.<sup>31,39</sup> The transition temperature from the  $Q_{II}^{D}$  to the  $H_{II}$  phase,  $T_{O_{II}II}$  increased a little with an increase in pH.

 $T_{Q\rightarrow H}$ , increased a little with an increase in pH. **3.2. Kinetics of the Low-pH-Induced L<sub>\alpha</sub> to Q<sub>II</sub><sup>D</sup> Phase Transition of 20%-DOPS/80%-MO at Various Temperatures. As described in our previous paper,<sup>27</sup> 20%-DOPS/ 80%-MO membranes at neutral pH are in the L<sub>\alpha</sub> phase (Figure S4(a)). First we conducted TR-SAXS experiments at a final pH of 2.6 at 20 °C. After the purified MLV suspension in buffer A was rapidly mixed with buffer C (pH 2.4) at 20 °C, the** 



**Figure 1.** Changes in structure and phase of 20%-DOPS/80%-MO membranes at low pH during a temperature scan from 20 to 50 °C at a rate of 1 °C/min (8.3 mM lipid concentration). (a) SAXS contour plot of the temperature scan at pH 2.7. (b) Averaged SAXS patterns of the data shown in (a) from 20.0 to 21.0 °C (bottom) and from 49.0 to 50.0 °C (top). (c) Temperature dependence of the lattice constants of the  $Q_{II}^{D}$  (in the upper figure) and of the  $H_{II}$  phases (in the lower figure). (black  $\bullet$ ,  $\bigcirc$ ) pH 2.6, (red  $\bullet$ ,  $\bigcirc$ ) pH 2.7, and (blue  $\bullet$ ,  $\bigcirc$ ) pH 2.8. (d) Temperature–pH phase diagram. (blue  $\bullet$ ) the  $Q_{II}^{D}$  phase, (green  $\blacksquare$ ) coexistence of the  $A_{II}$  phases, and (red  $\blacktriangle$ ) coexistence of the  $H_{II}$  phase and unidentified structure.

structure and the phase of the membranes in the resultant suspension (final pH 2.6) changed with time. The contour plot shows the time course of the SAXS patterns of this sample



**Figure 2.** Changes in structure and phase of 20%-DOPS/80%-MO membranes after the pH jump from pH 6.7 to pH 2.6 at various temperatures (7.5 mM lipid concentration). (a) SAXS contour plot of the time course at 20 (a), 30 (c), and 35 °C (d). (b) Averaged SAXS patterns of the data shown in (a) from 0.2 to 2 s (bottom), from 50 to 59 s (middle), and from 3620 to 3629 s (top). (e) Integrated intensity of the (10) peak of the H<sub>II</sub> phase; at 20 °C (black), at 25 °C (red), at 30 °C (blue), and at 35 °C (green).

(Figure 2a), and the waterfall plot of the same data is shown in Figure S5. From 0 to 10 s, only SAXS peaks corresponding to the  $L_{\alpha}$  phase were observed (Figure 2a,b). At 10 s after mixing, a new weak peak appeared at around  $S = 0.163 \text{ nm}^{-1}$ , and its intensity increased with time. The SAXS pattern at 50 s (Figure 2a,b) shows peaks which have a spacing ratio of  $1:\sqrt{3:2}$ , corresponding to an  $H_{II}$  phase, indicating that the peak at S =0.163 nm<sup>-1</sup> was due to the (10) peak of the  $H_{II}$  phase. The intensities of the peaks of the H<sub>II</sub> phase increased with time up to 50 s and then decreased (Figure 2e, black curve), whereas those of the  $L_{\alpha}$  phase became low at 50 s. At 100 s, two weak peaks at S = 0.107 and  $0.131 \text{ nm}^{-1}$  appeared, and their intensities increased with time. We also measured the SAXS pattern of the same sample following a long incubation (10 h at 25 °C) (Figure S4(b)); this pattern should correspond to the equilibrium structure. Peaks which have a spacing ratio of  $\sqrt{2}:\sqrt{3}:\sqrt{4}:\sqrt{6}:\sqrt{8}:\sqrt{9}$  were indexed as the (110), (111), (200), (211), (220), and (221) peaks of a Q<sub>II</sub><sup>D</sup> phase; its lattice constant was 11.5 nm. On the basis of the equilibrium structure, the peaks at S = 0.107 and  $0.131 \text{ nm}^{-1}$  in Figure 2a were assigned as the (110) and (111) peak of the  $Q_{II}^{D}$  phase, respectively.

The result of the same experiment at 30 °C (Figure 2c) shows that the peak of the H<sub>II</sub> phase appeared earlier but the peaks of the  $Q_{II}^{\ \ D}$  phase appeared later compared to those at 20 °C (Figure 2a). In contrast, at 35 °C (Figure 2d), the (10) peak of the  $H_{II}$  phase started to appear at 3 s, but the (110) and (111) peaks of the  $Q_{II}^{\ \ D}$  phase started to appear at ~1000 s. Figure 2e shows the time course of the intensity of the (10) peak of the H<sub>II</sub> phase at various temperatures, indicating that with an increase in temperature the  $H_{II}$  phase started to appear earlier. Especially at 35 °C, we observed only small peaks of the  $Q_{II}^{D}$  phase 1 h after mixing, indicating that the rate of the transition from the  $H_{II}$  to the  $Q_{II}^{D}$  phase was very slow (i.e., the membranes were almost trapped in the intermediate H<sub>II</sub> phase). The lattice constant of the H<sub>II</sub> phase decreased with temperature from 7.1 nm (at 20 °C) to 6.8 nm (35 °C) (Table 1).

We conducted the same TR-SAXS experiments at final pH values of 2.7 and 2.8 at various temperatures and obtained similar results. (See the quantitative analysis in the Discussion section.)

Table 1. Temperature Dependence of the Lattice Constants at Various pH Values<sup>a</sup>

temperature (°C)	${f L}_{lpha} \left( { m initial}  ight) \ ({ m nm})$	$H_{II}$ (intermediate) (nm)	$\begin{array}{c} Q_{II}^{D} (1 h) \\ (nm) \end{array}$
	(a) F	inal pH 2.6	
20	10	7.1	13.2
25	10	7.0	12.1
30	10	6.9	11.3
35	10	6.8	10.8
	(b) F	inal pH 2.7	
20	10	7.2	14.1
25	10	7.0	12.9
30	10	7.0	11.9
35	10	6.8	11.2
	(c) F	inal pH 2.8	
20	10		
25	10	7.1	13.7
30	10	7.0	12.5
35	10	6.9	11.8
a	D .		

<sup>a</sup>Lattice constants for the  $Q_{II}^{D}$  phase 1 h after mixing with the low-pH buffer were determined.

# 4. DISCUSSION

The results of the temperature scan of the SAXS measurements clearly show that for the 20%-DOPS/80%-MO membranes at low pH (2.6–2.8) the  $Q_{II}^{D}$  to  $H_{II}$  phase transition started to occur at 33–35 °C (depending on pH). This result agrees with the results of other cubic systems of lipid membranes.<sup>31,34,39</sup> In excess water, the membrane in the H<sub>II</sub> phase has a large negative curvature close to the spontaneous curvature,<sup>40,41</sup> and thereby the radius of the water cylinder in the  $H_{II}$  phase which is defined as the distance between the center of the water cylinder and the neutral surface of the monolayer,  $R_w$ , is almost the same as the radius of the spontaneous curvature,  $R_0$ . It is reported that the  $|H_0|$  of phosphatidylethanolamine (PE) monolayers increases with temperature.<sup>34,40,41</sup> As shown in Figure 1c, the lattice constant a of the  $H_{II}$  phase of 20%-DOPS/ 80%-MO decreased with temperature. In other lipid systems, a of the H<sub>II</sub> phase decreased with temperature.<sup>41</sup> Since a = 2 ( $R_w$  $(+ d_m)$  where  $d_m$  is the thickness of the monolayer and the temperature dependence of  $d_{\rm m}$  is very small,  $\Delta a \approx 2\Delta R_{\rm w}^{41}$ Thereby, the decrease in *a* with temperature indicates that  $R_w$ decreases with temperature; therefore,  $|H_0|$  of this monolayer increases with temperature (i.e.,  $H_0$  decreases with temperature). The free energy of the  $L_{\alpha}$  phase  $(G_{L_{\alpha}})$  of this membrane is large due to the curvature elastic energy,  $G_{\rm L}^{\rm curv}$  (=  $\kappa H_0^2 A/2$ , where  $\kappa$  is the bending modulus of monolayer and A is the area of membranes), since the mean curvature of the membrane in the  $L_{\alpha}$  phase is 0; therefore,  $G_{L_{\alpha}}$  increases with temperature. In contrast, the free energy of the  $H_{II}$  phase  $(G_{HII})$  due to the curvature elastic energy is very small, but G<sub>HII</sub> is large due to the interstitial chain packing energy of the  $H_{II}$  phase,  $G_{\rm HII}^{\rm pack 29,41,42}$  Hence, the difference between the free energy of the H<sub>II</sub> phase and that of the L<sub> $\alpha$ </sub> phase,  $\Delta G_{H-L}$  (=  $G_{HII} - G_{L\alpha}$ ) can be described as follows.<sup>29,41,42</sup>

$$\Delta G_{\rm H-L} = G_{\rm H_{II}} - G_{\rm L_{a}} = G_{\rm H_{II}}^{\rm pack} - \kappa H_0^{\ 2} A/2 \tag{1}$$

Therefore,  $\Delta G_{H-L}$  decreases with an increase in  $|H_0|^2$ , and  $\Delta G_{H-L} = 0$  at the transition temperature from the L<sub>a</sub> to the H<sub>II</sub> phases,  $T_{L \rightarrow H}$ .<sup>29,40,41</sup> On the other hand, the difference between

the free energy of the  $Q_{II}^{D}$  phase  $(G_{QII})$  and  $G_{L_{a'}} \Delta G_{Q-L}$  (=  $G_{QII} - G_{L_{a'}}$ ), can be described as follows.<sup>34,43,44</sup>

$$\Delta G_{Q-L} = G_{Q_{II}} - G_{L_{\alpha}} = \overline{\kappa}_{bil} \langle K \rangle A$$
  
where  $\overline{\kappa}_{bil} = 2(\overline{\kappa}_{m} - 4\kappa H_0 \xi)$  (2)

where  $\overline{\kappa}_{\rm bil}$  is the Gaussian curvature modulus of the bilayer,  $\langle K \rangle$  is the average value of the Gaussian curvature of the membrane over its total neutral surface area A,  $\overline{\kappa}_{\rm m}$  is the Gaussian curvature modulus of the monolayer, and  $\xi$  is the distance between the bilayer midplane and monolayer's neutral surface. Therefore,  $\Delta G_{\rm Q-L}$  decreases with an increase in  $|H_0|$ , and  $\Delta G_{\rm Q-L} = 0$  at the transition temperature from the  $L_{\alpha}$  to the  $Q_{\rm II}$  phases,  $T_{\rm L \rightarrow Q}$ .<sup>3,29,34</sup> If  $T_{\rm L \rightarrow Q}$  is less than  $T_{\rm L \rightarrow H_2}$  then as the temperature increases, phase transitions occur according to the phase sequence of  $L_{\alpha} \rightarrow Q_{\rm II} \rightarrow H_{\rm II}$ , and the  $Q_{\rm II}$  to  $H_{\rm II}$  phase transition occurs at  $T_{\rm Q \rightarrow H}$  when  $G_{\rm HII} = G_{\rm QII}$ .<sup>45</sup>

The lattice constant of the  $H_{II}$  phase (6.8 nm) which was observed initially after the  $Q_{II}^{D}$  to  $H_{II}$  phase transition during the temperature scan (i.e., at ~35 °C) (Figure 1c) is almost the same as that of the intermediate state of the low-pH-induced  $L_{\alpha}$ to  $Q_{II}^{D}$  phase transition of the 20%-DOPS/80%-MO membrane at 35 °C (6.8 nm, Table 1). This supports that the identification of the intermediate state as the  $H_{II}$  phase is valid.

The results of Figure 1 show that the lattice constant of the  $Q_{II}^{D}$  phase was almost constant from 20 to 31 °C at a heating rate of 0.5–1.0 °C/min but above 31 °C (before starting the transition) it decreased greatly with temperature. Recently, Barriga et al. reported that the binary mixture of MO with a small amount of DOPS or dioleoylphosphatidylglycerol (DOPG) in water under nonexcess water conditions (70 wt % water) shows an increase in the lattice constant with an increase in temperature.<sup>46</sup> This is an interesting difference, but currently we do not know its reason.

The results of TR-SAXS measurements clearly show the temperature dependence of the kinetic pathway of the low-pHinduced  $L_{\alpha}$  to  $Q_{II}^{D}$  phase transition of the 20%-DOPS/80%-MO membrane. Here, we analyze the kinetics of this phase transition quantitatively using the same method described in our previous paper.<sup>28</sup> In the low-pH-induced  $L_a$  to  $Q_{II}^{D}$  phase transition of the purified MLVs (e.g., Figure 2a), SAXS peaks due to each phase were well separated. We therefore applied the NMF method<sup>37,38</sup> to obtain the rate constant of each step of the phase transition. The results of the NMF method are shown in Figure 3. Figure 3a-c indicates three components in the data (i.e., the  $L_{\alpha}$  (a), the  $H_{II}$  (b), and the  $Q_{II}^{D}$  phases (c)). Figure 3d-f indicates the time course of each component. We can divide the time course into two stages. In the first stage up to around 50 s, the amount of the  $L_{\alpha}$  phase decreased, the  $H_{\rm II}$ phases increased, and the Q<sub>II</sub><sup>D</sup> phase remained almost 0. Most of the membranes in the  $L_{\alpha}$  phase, therefore, were converted to the  $H_{II}$  phase. In the second stage from 50 to 3629 s, the amount of the  $H_{II}$  phase decreased but that of the  $Q_{II}{}^{\rm D}$  phase increased. Therefore, in the second stage, the phase transition occurred from the  $H_{II}$  to the  $Q_{II}{}^{\rm D}$  phase. To fit the data of the decrease in intensity of the  $H_{II}$  phase (Figure 3e), two rate constants were required for the  $H_{II}$  to  $Q_{II}^{D}$  phase transition; one is for the fast transition from the  $H_{II}$  to the  $Q_{II}^{\ D}$  phase  $(k_{2\rm F})$ , and the other is for the slow transition from the  ${
m H_{II}}$  to the  $Q_{II}^{D}$  phase ( $k_{2S}$ ). The basic scheme of the phase transitions is as follows.



**Figure 3.** Results from the MALS calculations of the SAXS pattern of a 20%-DOPS/80%-MO membrane suspension from 0.2 to 3629 s after the pH jump from 6.7 to 2.6 at 30 °C (Figure 2c). Restored SAXS profiles of matrix *A* corresponding to the  $L_{av}$  H<sub>II</sub>, and Q<sub>II</sub><sup>D</sup> phases are shown in a–c, respectively. The time courses of the SAXS intensities of matrix *B* corresponding to the  $L_{av}$  H<sub>II</sub>, and Q<sub>II</sub><sup>D</sup> phases are shown in d–f, respectively.

$$\begin{array}{ccc} \mathrm{L}_{\alpha} \xrightarrow{k_{1}} \mathrm{H}_{\mathrm{II}} \xrightarrow{k_{2\mathrm{F}}} \mathrm{Q}_{\mathrm{II}}^{\mathrm{D}} \mbox{ (fraction } p \mbox{ of the } \mathrm{H}_{\mathrm{II}} \mbox{ phase}) \\ & \xrightarrow{k_{2\mathrm{S}}} \mathrm{Q}_{\mathrm{II}}^{\mathrm{D}} \mbox{ (fraction } (1-p) \mbox{ of the } \mathrm{H}_{\mathrm{II}} \mbox{ phase}) \end{array}$$
(3)

where  $k_1$  is the rate constant of the transition from the  $L_{\alpha}$  to the  $H_{II}$  phase. The time courses of the concentration of each phase are described using the following differential equations.

Table 2. pH Dependence of the Rate Constants

$$\frac{d[L_{\alpha}]}{dt} = -k_{1}[L_{\alpha}]$$

$$\frac{d[H_{II}]}{dt} = k_{1}[L_{\alpha}] - \{pk_{2F} + (1-p)k_{2S}\}[H_{II}]$$

$$\frac{d[Q_{II}^{D}]}{dt} = \{pk_{2F} + (1-p)k_{2S}\}[H_{II}]$$
(4)

The solutions for these differential equations under the initial condition  $([L_{\alpha}] = C_0 \text{ at } t = 0)$  are as follows.

$$\begin{split} & [\mathrm{L}_{a}] = C_{0} \exp(-k_{1}t) \\ & [\mathrm{H}_{\mathrm{II}}] = \frac{k_{1}C_{0}}{\{pk_{2\mathrm{F}} + (1-p)k_{2\mathrm{S}}\} - k_{1}} [\exp(-k_{1}t) \\ & - \exp[-\{pk_{2\mathrm{F}} + (1-p)k_{2\mathrm{S}}\}t]] \\ & [\mathrm{Q}_{\mathrm{II}}^{\mathrm{D}}] = \frac{k_{1}C_{0}\{pk_{2\mathrm{F}} + (1-p)k_{2\mathrm{S}}\}}{\{pk_{2\mathrm{F}} + (1-p)k_{2\mathrm{S}}\} - k_{1}} [k_{1}\exp[-\{pk_{2\mathrm{F}} + (1-p)k_{2\mathrm{S}}\}t] \\ & - \{pk_{2\mathrm{F}} + (1-p)k_{2\mathrm{S}}\}\exp(-k_{1}t) + k_{1}C_{0}\{pk_{2\mathrm{F}} + (1-p)k_{2\mathrm{S}}\}\} \end{split}$$
(5)

The time courses in Figure 3 are not the fractions of components, and the values might not start from or end at 0. We modified the equations as follows.

$$\begin{split} & [L_{a}] = A_{0} \exp(-k_{1}t) + B_{0} \\ & [H_{II}] = A_{1} \{ \exp(-k_{1}t) - \exp[-\{pk_{2F} + (1-p)k_{2S}\}t] \} + B_{1} \\ & [Q_{II}^{D}] = A_{2} \{ k_{1} \exp[-\{pk_{2F} + (1-p)k_{2S}\}t] - \{pk_{2F} + (1-p)k_{2S}\} \\ & \exp(-k_{1}t) \} + B_{2} \end{split}$$

$$(6)$$

The time course of the SAXS intensities of the three phases for the data of Figure 2c (final pH 2.6 at 30 °C) was fit well by eq 6 (Figure 3d-f), providing  $k_1 = 0.081 \text{ s}^{-1}$ ,  $k_{2F} = 0.0050 \text{ s}^{-1}$ ,  $k_{2S} = 0.00031 \text{ s}^{-1}$ , and p = 0.35. As shown in Table 2, values of  $k_1$  were 2–17 times larger than those of  $k_{2F}$  at same pH and temperature. It is noted that the accuracy of the values of  $k_{2S}$ was not high because the measuring time was 3600 s, which is

(a) $k_1 (s^{-1})^{\alpha}$							
	pH 2.6		pH 2.7	pH 2.8			
20 °C	0.036	$2 \pm 0.0008$	$0.0175 \pm 0.0004$	ND			
25 °C	0.072	$\pm 0.001$	$0.058 \pm 0.001$	$0.0041 \pm 0.0001$			
30 °C	0.081	$\pm 0.001$	$0.068 \pm 0.001$	$0.019 \pm 0.0004$			
35 °C	ND		ND	$0.033 \pm 0.0005$			
(b) $k_{2F}^{\ b} k_{2S}^{\ c}$ and $p^d$							
		pH 2.6	рН 2.7	pH 2.8			
20 °C	$k_{2\rm F}~({\rm s}^{-1})$	$0.0055 \pm 0.0002$	$0.0043 \pm 0.0006$	ND			
	$k_{2S}$ (s <sup>-1</sup> )	$0.00018 \pm 0.00002$	$0.00072 \pm 0.00002$	ND			
	р	$0.71 \pm 0.01$	$0.38 \pm 0.03$	ND			
25 °C	$k_{2\rm F}~({\rm s}^{-1})$	$0.0043 \pm 0.0001$	$0.0048 \pm 0.0002$	$0.0022 \pm 0.0002$			
	$k_{2S} (s^{-1})$	$0.00024 \pm 0.00002$	$0.00033 \pm 0.00002$	$0.00011 \pm 0.00006$			
	р	$0.62 \pm 0.01$	$0.60 \pm 0.01$	$0.87 \pm 0.02$			
30 °C	$k_{2\rm F}~({ m s}^{-1})$	$0.0050 \pm 0.0002$	$0.0067 \pm 0.0003$	$0.0024 \pm 0.0001$			
	$k_{2S} (s^{-1})$	$0.00031 \pm 0.00001$	$0.00071 \pm 0.00001$	$0.00016 \pm 0.00002$			
	р	$0.35 \pm 0.01$	$0.44 \pm 0.01$	$0.66 \pm 0.02$			
35 °C	$k_{2\rm F}~({\rm s}^{-1})$	ND	ND	$0.0032 \pm 0.0002$			
	$k_{2S} (s^{-1})$	ND	ND	$0.00028 \pm 0.00001$			
	р	ND	ND	$0.35 \pm 0.01$			

<sup>*a*</sup>Rate constants of the initial step (i.e., the  $L_{\alpha}$  to  $H_{II}$  phase transition). <sup>*b*</sup>Rate constants of the fast transition from the  $H_{II}$  to the  $Q_{II}^{D}$  phase. <sup>*c*</sup>Rate constant of the slow transition from the  $H_{II}$  to the  $Q_{II}^{D}$  phase. <sup>*d*</sup>Fraction of the  $H_{II}$  phase which follows the fast transition.

not sufficient to determine accurate values of  $k_{2S}$ . At present, we do not know the origin of the slower component of the H<sub>II</sub> to the Q<sub>II</sub><sup>D</sup> phase transition ( $k_{2S}$ ). The rate constant of the second step may depend on the size of the membranes.

Next we consider the temperature dependence of the rate constants of both steps. The  $k_1$  values greatly increased with temperature for all pH values. Figure 4a shows the graphs of



**Figure 4.** Temperature dependence of the rate constant. (a)  $\log_{10} k_1$  vs 1/T at final pH 2.6 (black), at pH 2.7 (red), and at pH 2.8 (blue). The inset is the pH dependence of the apparent activation energy,  $E_a$  ( $L_{\alpha} \rightarrow H_{\rm II}$ ). (b)  $\log_{10} k_2$  vs 1/T at final pH 2.6 (black), at pH 2.7 (red), and at pH 2.8 (blue). The inset is the pH dependence of the apparent activation energy,  $E_a$  ( $H_{\rm II} \rightarrow Q_{\rm II}^{\rm D}$ ).

 $\log_{10} k_1$  vs 1/T (where T is absolute temperature) at various pH values. Since  $k = A \exp(-E_a/RT)$ , where  $E_a$  is apparent activation energy, R is the gas constant, and A is a constant called the pre-exponential factor, the value of  $E_{\rm a}$  can be determined using an equation of  $-2.30R \times (slope of the curve$ of  $\log_{10} k$  vs 1/T). As the temperature increased from 20 to 35 °C, the pH of the suspension changed by less than 0.5 (Figure S3). At all pH values, the data were well fit linearly, indicating that  $E_a (L_{\alpha} \rightarrow H_{II})$  does not depend on temperature (i.e., it is constant). Therefore, we were able to obtain the values of  $E_a$  $(L_{\alpha} \rightarrow H_{II})$  by the slope of the curves. The value of  $E_a$   $(L_{\alpha} \rightarrow$  $H_{II}$ ) increased with an increase in pH from 60 ± 20 kJ/mol at pH 2.6 to 160  $\pm$  40 kJ/mol at pH 2.8 (Figure 4a inset). The appearance of the intermediate H<sub>II</sub> phase in the low-pHinduced  $L_{\alpha}$  to  $Q_{II}^{D}$  phase transition can be explained by a greater activation energy of the direct transition from the  $L_{\alpha}$  to  $Q_{II}^{D}$  phase,  $E_a (L_{\alpha} \rightarrow Q_{II}^{D})$ , than  $E_a (L_{\alpha} \rightarrow H_{II})$ . As shown in Table 2a,  $k_1$  increased greatly with a decrease in pH at same temperature, which can be explained by the decrease in  $E_a$  (L<sub> $\alpha$ </sub>  $\rightarrow$  H<sub>II</sub>) with a decrease in pH (Figure 4a). Here we did not make a correction to the pH (i.e., the pH in Figure 4 is the pH at 20 °C) but considered it to be an experimental error of the values of  $E_a$ . We estimated the corrected values of  $E_a$  (i.e.,  $E_a'$ ) by using the corrected rate constants of the same pH determined by the linear interpolation of the values of the rate constants at the same 1/T. These values of  $E_a'$  were a little

smaller than those of  $E_a$  without correction, but the  $E_a'$  values existed within the experimental error of the  $E_a$  values in the insets of Figure 4 (details in SI).

In the process of the  $L_{\alpha}$  to  $H_{II}$  phase transition, at first the neighboring bilayers in the  $L_{\alpha}$  phase must contact each other at a local site due to their thermal fluctuation (Figure S8a), and then the apposed (cis) monolayers fuse to form stalk structures (or the trans monolayer contact) (Figure S8b).<sup>47,48</sup> We consider that the stalk structures involve the transition state, which determines  $E_{\rm a}$  ( $L_{\alpha} \rightarrow H_{\rm II}$ ). The surface charge density of the DOPS/MO membrane increases with an increase in pH because the protonation of the carboxylic acid of DOPS becomes smaller at higher pH. Therefore, we can reasonably consider that the electrostatic interactions inside the membrane in the stalk structure increase with an increase in pH, resulting in the increase in  $E_{\rm a}$  ( $L_{\alpha} \rightarrow H_{\rm II}$ ).

In contrast, the value of  $k_{\rm 2F}$  decreased slightly with temperature for pH 2.6, although the  $k_{2F}$  values for pH 2.7 and 2.8 slightly increased with temperature (Table 2b). We obtained the values of  $E_a$  ( $H_{II} \rightarrow Q_{II}^{D}$ ) by the slope of the curves at pH 2.7 and 2.8 (Figure 4b). The result at pH 2.6 indicates that  $E_a$  ( $H_{II} \rightarrow Q_{II}^{(D)}$ ) increases with temperature. On the other hand,  $E_a$  ( $H_{II} \rightarrow Q_{II}^{(D)}$ ) at pH 2.7 and 2.8 was 30 ± 10 kJ/mol (Figure 4b inset). These values of  $E_a$  ( $H_{II} \rightarrow Q_{II}^{D}$ ) were smaller than those of  $E_a$  ( $L_{\alpha} \rightarrow H_{II}$ ) at the same pH. However, the values of  $k_1$  were greater than those of  $k_{2F}$  at same pH (Table 2). Therefore, we conclude that the pre-exponential factor of the rate constant of the second step (i.e., the  $H_{II}$  to  $Q_{II}^{D}$  phase transition) is much smaller than that of the first step (i.e., the  $L_{\alpha}$  to  $H_{II}$  phase transition). In other words, the frequency of the attempt of the  $H_{II}$  to  $Q_{II}^{\ D}$  phase transition is much smaller than that of the  $L_{\alpha}$  to  $H_{II}$  phase transition. As described above, the stalk structures involve the transition state from the L<sub>a</sub> to H<sub>II</sub> phase transition, which determines  $E_a$  (L<sub>a</sub>  $\rightarrow$  $H_{II}$ ). The thermal fluctuation of bilayer in the  $L_{\alpha}$  phase is so large that the attempt to form local contacts between neighboring membranes occurs frequently and hence the preexponential factor of the  $L_{\alpha}$  to the  $H_{II}$  phase transition is much greater than that of the  $H_{II}$  to  $Q_{II}^{D}$  phase transition.

In the present study, we obtained the values of the apparent activation energy of the elementary steps of the low-pHinduced  $L_{\alpha}$  to  $Q_{II}^{D}$  phase transition in 20%-DOPS/80%-MO. The values of  $E_a$  ( $L_{\alpha} \rightarrow H_{II}$ ) were 60–160 kJ/mol, and those of  $E_{\rm a}$  (H<sub>II</sub>  $\rightarrow$  Q<sub>II</sub><sup>D</sup>) were 30 kJ/mol. To our knowledge, the values of the activation energies of the  $L_{\alpha}$  to  $H_{II}$  phase transition and the  $H_{II}$  to  $Q_{II}^{D}$  phase transition of lipid membranes have never been published; therefore, it is difficult to compare these values with those of other lipid membranes. During the phase transitions from  $L_{\alpha}$  to  $H_{II}$  and from  $H_{II}$  to  $Q_{II}^{D}$ , the rupture of the membrane must occur because these phases are topologically different. It is considered that during the  $L_{\alpha}$  to  $H_{II}$  (or  $Q_{II}^{D}$ ) phase transition after the trans monolayer contact (TMC) or hemifusion intermediate is produced (Figure S8c), there are two patterns of structural changes from the TMC.<sup>48</sup> If the trans monolayers at the TMC rupture, then an interlamellar attachment (ILA) or a fusion pore (Figure S8e) is formed (type A). If ILAs accumulate in sufficient numbers, they form ILA lattices, which are transient intermediates in Q<sub>II</sub> phase formation. If rupture does not occur and TMCs accumulate and aggregate, the  $H_{II}$  phase appears (Figure S8d) (type B). The rate of bilayer rupture determines the relative rate of  $H_{II}$ phase formation.<sup>48</sup> Recently, the activation energies of the tension ( $\sigma$ )-induced rupture of the bilayer,  $E_a$  (rupture), have

been determined; in the case of the electrically neutral dioleoylphosphatidylcholine (DOPC) bilayer,  $E_a$  (rupture) = 49 kJ/mol at  $\sigma$  = 7.0 mN/m and  $E_a$  (rupture) decreased with an increase in tension.<sup>49</sup> It is considered that  $E_a$  (rupture) decreases greatly with an increase in the electrostatic interactions due to surface charges of the bilayer.<sup>50</sup> Since the 20%-DOPS/80%-MO membrane is a charged membrane, we can expect that  $E_a$  (rupture) is smaller but increases with a decrease in pH. Therefore, we can consider that  $E_a$  ( $L_a \rightarrow H_{II}$ ) is larger than  $E_a$  (rupture) but  $E_a$  ( $H_{II} \rightarrow Q_{II}^{D}$ ) is similar to  $E_a$  (rupture).

The rate constant of the initial step,  $k_1$ , increased with temperature. By analyzing this result using the standard method, we obtained the values of  $E_a$  ( $L_{\alpha} \rightarrow H_{II}$ ), which did not change with temperature. As described above, the free energy of the  $L_{\alpha}$  phase  $(G_{L_{\alpha}})$  of this membrane increases with temperature due to the increase in  $|H_0|$ . Therefore, we can infer that the free energy of the transition state from the  $L_{\alpha}$  phase to the H<sub>II</sub> phase,  $G^{\ddagger}$  (L<sub> $\alpha$ </sub>  $\rightarrow$  H<sub>II</sub>), increases with temperature so that  $E_a (L_{\alpha} \rightarrow H_{II})$  becomes constant with temperature. However, when we consider the phase transitions or the reactions whose transition state's free energy depends on temperature, we need a suitable theory for its activation energy. Squires et al. proposed a quantitative theory of the activation energy  $\Delta G^{\ddagger}(T)$  of phase transitions of lipid membranes from phase A to phase B involving changes in monolayer curvature.<sup>35</sup> This theory can reasonably explain the pressure (P)-induced phase transition between Q<sub>II</sub><sup>D</sup> and Q<sub>II</sub><sup>P</sup>. They assumed that the activation energy is determined only by the change in the curvature elastic energy and thereby obtained the following equation.

$$\Delta G^{\ddagger}(T) = G^{\ddagger} - G_{A} = \Delta G^{\ddagger'} + N_{A} N_{coop} A_{n}$$

$$\{ (g^{\ddagger}(T) - g^{\ddagger'}) - (g_{A}(T) - g_{A}^{\phantom{A}'}) \}$$
(7)

where  $G^{\ddagger}$  is the free energy of the transition state;  $\Delta G^{\ddagger}'$  is the activation energy at the phase boundary between phases A and B, where the free energy of both phases are the same,  $G_A = G_B$ ;  $N_A$  is Avogadro's number;  $N_{coop}$  is the number of molecules in a cooperative unit;  $A_n$  is the cross-sectional area per molecule at the pivotal surface;  $g^{\ddagger}(T)$  and  $g^{\ddagger'}$  are the curvature elastic energy per unit area of the transition state at T and at the phase boundary, respectively; and  $g_A(T)$  and  $g_A'$  are the curvature elastic energy per unit area of phase A at T and at the phase boundary, respectively. For the equation of g, the Helfrich's expression<sup>51</sup> is used as follows.

$$g = 2\kappa (H - H_0)^2 + \overline{\kappa}_{\rm m} K$$

If we assume that Gaussian curvature *K* and  $\kappa$  are constants (i.e., not depend on temperature), then eq 7 is converted to the following equation<sup>35</sup>

$$\Delta G^{\ddagger}(T) = G^{\ddagger} - G_{A} = \Delta G^{\ddagger'} + 2\kappa N_{A} N_{coop}$$

$$A_{n} \{ (H^{\ddagger} - H_{0})^{2} - (H^{\ddagger'} - H_{0}')^{2} - (H_{A} - H_{0})^{2} + (H_{A}' - H_{0}')^{2} \}$$
(8)

where  $H^{\ddagger}$  and  $H_{A}$  are the mean curvature of the transition state and phase A, respectively, and ' denotes the physical quantity at the phase boundary. Squires et al. assumed that  $H^{\ddagger}$  and  $H_{A}$  are constants (i.e., not depend on temperature) because their membrane systems were under limited hydration conditions.<sup>35</sup> In this case, eq 8 can be converted to the following equation, which is the main equation in the theory of Squires et al.<sup>35</sup>

$$\Delta G^{\ddagger} = \Delta G^{\ddagger'} - 4\kappa N_{\rm A} N_{\rm coop} A_{\rm n} (H_0 - H_0') (H^{\ddagger} - H_{\rm A}) \quad (9)$$

However, in our case we investigated DOPS/MO membranes in excess water, and hence it is difficult to adopt the assumption of Squires et al. The result of Figure 1c clearly shows that the mean curvature of the  $H_{II}$  phase,  $H_{H_{II}}$ , decreases with an increase in temperature, which supports our consideration. Therefore, we consider here that  $H^{\ddagger}$  and  $H_{A}$  depend on temperature, and as a result we use eq 8 instead of eq 9.

First we consider the initial step of the low-pH-induced  $L_{\alpha}$  to  $Q_{II}^{\ \ D}$  phase transition in 20%-DOPS/80%-MO (i.e., the  $L_{lpha}$  to  $H_{II}$  phase transition). In this case, phase A is the  $L_{\alpha}$  phase and phase B is the H<sub>II</sub> phase, and both the phases are stable or metastable states, which have a free-energy minimum. We consider that another stable state does not exist during the  $L_{\alpha}$ to H<sub>II</sub> phase transition. However, as we described above, during the  $L_{\alpha}$  to  $H_{II}$  phase transition there are many transient, unstable states such as membranes containing the stalk, the TMC, and the close contact at local sites (Figure S6), and the most unstable state which has the highest free energy is called the transition state. As defined in eq 7, the activation energy from the  $L_{\alpha}$  to  $H_{II}$  phase transition is defined as the difference between the free energy of the transition state and that of the  $L_{\alpha}$  phase; therefore, the activation energy does not depend on many unstable states during the reaction path from the  $L_{\alpha}$  to the H<sub>II</sub> phase. Since phase A is the L<sub> $\alpha$ </sub> phase, H<sub>A</sub> = H<sub>L<sub> $\alpha</sub></sub> = 0. We</sub></sub>$ assume that the mean curvature of the transition state  $H^{\ddagger}$  of the  $L_{\alpha}$  to  $H_{II}$  phase transition can be expressed by the first-order approximation of temperature in the small temperature range, and hence  $H^{\ddagger}$  (L<sub> $\alpha$ </sub>  $\rightarrow$  H<sub>II</sub>) = C<sub>1</sub> +  $\beta$ T, where C<sub>1</sub> and  $\beta$  are constants. On the other hand, it is well known that  $H_0$  of lipid membranes decreases linearly with temperature.<sup>35,44,52,53</sup> Here we also assume that  $H_0$  of the 20%-DOPS/80%-MO monolayer decreases linearly with temperature (i.e.,  $H_0 = -C_0 - \alpha T$ , where  $C_0$  and  $\alpha$  are positive constants). Therefore,  $H_0 - H_0' = -\alpha \Delta T$ , where  $\Delta T = T - T'$  and T' is the temperature at the phase boundary or the phase-transition temperature. Using eq 8, we can obtain the activation energy of this phase transition,  $\Delta G^{\ddagger}$  $(L_{\alpha} \rightarrow H_{II})$ , as follows.

$$\Delta G^{\ddagger} (L_{\alpha} \to H_{\mathrm{II}}) = \Delta G^{\ddagger\prime} (L_{\alpha} \to H_{\mathrm{II}}) + 2\kappa N_{\mathrm{A}} N_{\mathrm{coop}} A_{n} \{ \beta^{2} T^{2} + D_{\mathrm{I}} (T - T^{\prime}) - \beta^{2} T^{\prime} T \}$$

$$(10)$$

where

$$D_{1} = 2C_{1}\beta + \beta^{2}T' + 2C_{1}\alpha - 2\beta H_{0} + 2\alpha\beta$$

As described in the Result section, we obtained the apparent activation energy by the slope of the curve of  $\ln k$  vs 1/T as follows.

$$\frac{\partial \ln k}{\partial (1/T)} = -\frac{\Delta G^{\ddagger}}{R} + \frac{T}{R} \left( \frac{\partial \Delta G^{\ddagger}}{\partial T} \right)$$
$$= -\frac{\left( \Delta G^{\ddagger \prime} - 2\kappa N_{\rm A} N_{\rm coop} A_n T' (\beta^2 T^2 + D_1) \right)}{R} \tag{11}$$

Therefore, the apparent activation energy of the initial step,  $E_a$   $(L_{\alpha} \rightarrow H_{II})$ , which was determined by the experimental results

shown in Figure 4a, is related to the theoretical activation energy,  $\Delta G^{\dagger'}$  ( $L_{\alpha} \rightarrow H_{II}$ ), as follows.

$$E_{a}(L_{\alpha} \rightarrow H_{II}) = \Delta G^{\mp \prime}(L_{\alpha} \rightarrow H_{II}) - 2\kappa N_{A} N_{coop} A_{n} T'$$
$$(\beta^{2} T^{2} + D_{I})$$
(12)

To agree with the experimental results of the temperature dependence of  $k_1$ , the value of  $E_a$  ( $L_\alpha \rightarrow H_{II}$ ) must be constant, and hence  $\beta = 0$  (i.e., the mean curvature of transition state  $H^{\ddagger}$  ( $L_\alpha \rightarrow H_{II}$ ) is constant,  $H^{\ddagger}$  ( $L_\alpha \rightarrow H_{II}$ ) =  $C_1$ ). In this case, eq 12 can be converted to the following equation,

$$\begin{split} E_{a}(L_{\alpha} \to H_{II}) &= \Delta G^{\dagger}{}'(L_{\alpha} \to H_{II}) - 4\kappa N_{A} N_{coop} A_{n} \alpha T' \\ H^{\dagger}(L_{\alpha} \to H_{II}) \end{split}$$
(13)

Equation 13 can also be obtained from eq 9. We can reasonably consider that  $H^{\ddagger}$  ( $L_{\alpha} \rightarrow H_{II}$ ) is negative if the stalk structure involves the transition state. In this case,  $E_{a}$  ( $L_{\alpha} \rightarrow H_{II}$ ) >  $\Delta G^{\ddagger \prime}$  ( $L_{\alpha} \rightarrow H_{II}$ ). If  $H^{\ddagger}$  ( $L_{\alpha} \rightarrow H_{II}$ )  $\approx 0$ , then  $E_{a}$  ( $L_{\alpha} \rightarrow H_{II}$ )  $\approx \Delta G^{\ddagger \prime}$  ( $L_{\alpha} \rightarrow H_{II}$ ).

In contrast, values of the rate constant of the second step,  $k_2$ , decreased with an increase in temperature for pH 2.6, although the  $k_2$  values slightly increased with temperature at pH 2.7 and 2.8, and its analysis provides the values of  $E_a$  ( $H_{II} \rightarrow Q_{II}^D$ ) (Figure 4b). The former results indicate that  $E_a$  ( $H_{II} \rightarrow Q_{II}^D$ ) at pH 2.6 is negative. From the result of Figure 1c and the first-order approximation of temperature, we can consider that  $H_{HII} = -C_2 - \beta T$ , where  $C_2$  and  $\beta$  are positive constants. We assume that the mean curvature of the transition state can be expressed similarly (i.e.,  $H^{\ddagger} = -C_3 - \gamma T$ , where  $C_3$  and  $\gamma$  are positive constants). Using eq 8, we can obtain the activation energy of this phase transition,  $\Delta G^{\ddagger}$  ( $H_{II} \rightarrow Q_{II}^D$ ), as follows.

$$\begin{split} \Delta G^{\ddagger} (\mathbf{H}_{\mathrm{II}} \rightarrow \mathbf{Q}_{\mathrm{II}}^{\mathrm{D}}) &= \Delta G^{\ddagger \prime} (\mathbf{H}_{\mathrm{II}} \rightarrow \mathbf{Q}_{\mathrm{II}}^{\mathrm{D}}) \\ &+ 2\kappa N_{\mathrm{A}} N_{\mathrm{coop}} A_{n} \Big[ \Big\{ \left(\alpha - \gamma\right)^{2} - \left(\alpha - \beta\right)^{2} \Big\} T^{2} + 2 \Big\{ \left(\alpha - \gamma\right) (C_{0} - C_{3}) \\ &- \left(\alpha - \beta\right) (C_{0} - C_{2}) T + D_{2} \Big] \end{split}$$

where

$$D_{2} = (C_{0} - C_{3})^{2} - (C_{0} - C_{2})^{2} - (H^{\ddagger \prime} - H_{0}')^{2} + (H_{A}' - H_{0}')^{2}$$
  
= const

From the slope of the curve of  $\ln k \text{ vs } 1/T$ ,  $E_a (H_{II} \rightarrow Q_{II}^D)$  can be obtained as follows.

$$E_{a}(H_{II} \to Q_{II}^{\ D}) = \Delta G^{\ddagger'}(H_{II} \to Q_{II}^{\ D}) + \{(\alpha - \beta)^{2} - (\alpha - \gamma)^{2}\}T^{2} + D_{2}$$
(15)

To agree with the experimental results at pH 2.6 (i.e., the rate constant decreased with temperature), the value of  $E_a$  ( $H_{\rm II} \rightarrow Q_{\rm II}^{\rm D}$ ) at pH 2.6 must be negative, and hence  $(\alpha - \beta)^2 < (\alpha - \gamma)^2$ . Generally, the absolute value of  $H_0$  is larger than that of the  $H_{\rm II}$  phase and the transition state. Therefore,  $|\alpha - \beta| < |\alpha - \gamma|$ . This indicates that the difference between the temperature dependence of the curvature of the transition state and  $H_0$  is greater than that between that of the curvature of the initial state (i.e., the  $H_{\rm II}$  phase) and  $H_0$ . Therefore, as temperature increases,  $\Delta G^{\ddagger}$  ( $H_{\rm II} \rightarrow Q_{\rm II}^{\rm D}$ ) increases greatly, and as a result the rate constant decreases with temperature. In contrast, to agree with the experimental results at pH 2.7 and 2.8 (i.e., the rate constant increased with temperature), the values of  $E_a$  ( $H_{\rm II} \rightarrow Q_{\rm II}^{\rm D}$ ) at pH 2.7 and 2.8 must be constant, and hence  $\beta = \gamma$ .

curvature of the transition state is the same as that of the  $H_{\rm II}$  phase at pH 2.7 and 2.8. This pH dependence may be explained by the change in the electrostatic interactions due to the surface charge density of the membrane.

It is instructive to describe the general relationship between  $\Delta G^{\ddagger}$  and  $E_a$  of a phase transition. When  $\Delta G^{\ddagger} = c$  (where *c* is a positive constant),  $E_a = c$  (>0) and therefore the rate constant of the phase transition, *k*, increases with temperature, which can be applied to most cases. When  $\Delta G^{\ddagger} = bT$  (where *b* is a positive constant),  $E_a = 0$  and therefore *k* does not change with temperature. When  $\Delta G^{\ddagger} = aT^2$  (where *a* is a positive constant),  $E_a = -aT^2$  and therefore *k* decreases with temperature. When  $\Delta G^{\ddagger} = aT^2 + bT + c$ ,  $E_a = -aT^2 + c$  and therefore the sign of  $E_a$  depends on the values of *a*, *c*, and *T*.

Schöppe et al. obtained the apparent activation energies of the gel  $(L_{\beta})$  to  $L_{\alpha}$  phase transitions and the  $L_{\beta}$  to  $H_{II}$  phase transition of glycolipid membranes, which were 150-190 kJ/mol.<sup>54</sup> They considered that a specific number of lipid molecules (i.e., the number of molecules in a cooperative unit,  $N_{coop}$ ) are involved in these phase transitions of lipid membranes cooperatively.<sup>35,54</sup> Squires et al. determined the value of  $N_{coop}$  of the transition between the  $Q_{II}^{G}$  and  $Q_{II}^{D}$ phases<sup>34</sup> by the analysis of the results of the *P*-jump TR-SAXS experiments<sup>55</sup> using the data of the rate constant of the reverse transition;  $N_{coop}$  was  $(3-6) \times 10^3$ . This indicates that several thousand molecules undergo the  $Q_{II}^{\ G} - Q_{II}^{\ D}$  phase transition cooperatively within one "cooperative unit", which is equal to 1–2 unit cells of  $Q_{II}^{G}$  or 4–10 unit cells of  $Q_{II}^{D,35}$  In the present study,  $N_{\rm coop}$  for both steps of the low-pH-induced  ${\rm L}_{\alpha}$  to  $Q_{II}^{D}$  phase transition in 20%-DOPS/80%-MO could not be determined. This phase transition was reversible; the addition of neutral buffer induced the phase transition from  $Q_{II}^{\ \ D}$  to  $L_{\alpha}^{\ \ -1}$ However, we have not yet succeeded in measuring its rate constant of this reverse phase transition using the stopped flow apparatus because we could not get a uniform suspension of these cubic-phase membranes at low pH, which is essential for the stopped flow experiments.

It is instructive to consider other phase transitions where an intermediate H<sub>II</sub> phase appeared. Squires et al. found the intermediate, transient H<sub>II</sub> phase during the P-jump-induced  $Q_{II}^{G}$  to  $Q_{II}^{D}$  phase transition in a mixture of lauric acid and dilauroylphosphatidylcholine (2:1) from 600 to 240–360 bar at 50 wt % water.<sup>56</sup> The authors proposed a hypothesis that the intermediate  $H_{II}$  phase is a temporary "water donor" because the water content of the  $Q_{II}^{\ D}$  phase is larger than that of the Q<sub>II</sub><sup>G</sup> phase at the phase transition. We tested this water donor hypothesis in our case (i.e., the low-pH-induced phase transition). We calculated the volume fraction of water,  $\Phi_{w}$ , in each phase. (See the detailed calculation in the SI.) For the case of the 20%-DOPS/80%-MO membrane at pH 2.6 and 25  $^{\circ}$ C,  $\Phi_{\rm W}$  of the L<sub>a</sub>, H<sub>II</sub>, and Q<sub>II</sub> <sup>D</sup> phases are 0.66, 0.23, and 0.48, respectively. Therefore, it is difficult to apply the water donor hypothesis to the low-pH-induced  $L_{\alpha}$  to  $Q_{II}^{\ D}$  phase transition. Cherezov et al. found in the temperature (T)-jump-induced  $L_{\alpha}$ to Q<sub>II</sub><sup>D</sup> phase transition in N-monomethylated dioleoylphosphatidylethanolamine (DOPE-Me) at a final temperature of 61 to 65  $^\circ\text{C}$  that a metastable  $H_{II}$  phase formed initially and disappeared very slowly while the Q<sub>II</sub> phase developed; after 3 h of incubation, both phases coexisted. 57 The kinetic pathway for this system is similar to that of our DOPS/MO system, although the rate constant of the  $L_{\alpha}$  to  $Q_{II}{}^{\rm D}$  phase transition in our system is much larger than that of the T-jump transition in DOPE-Me. Recently, Siegel and Tenchov proposed to add the unbinding energy of the  $L_{\alpha}$  phase,  $g_{w}$  to the free energy of each phase and succeeded in explaining the relative stability of each phase using their new theory; when  $g_{\mu}$  of the lipid membrane is small, then  $T_{\mathrm{L} \rightarrow \mathrm{Q}}$  is lower than  $T_{\mathrm{L} \rightarrow \mathrm{H}}$  and therefore the membrane exhibits the phase sequence  $L_{\alpha} \rightarrow Q_{II} \rightarrow H_{II}$  as temperature increases (e.g., DOPE-Me), but when  $g_u$  is large,  $T_{L \rightarrow Q}$  is greater than  $T_{L \rightarrow H}$  and therefore a direct  $L_{\alpha}$  to  $H_{II}$ phase transition occurs (i.e., the Q<sub>II</sub> phase is metastable).<sup>45</sup> However, this theory cannot explain the appearance of the metastable H<sub>II</sub> phase in the T-jump in DOPE-Me membranes.<sup>57</sup> On the other hand, when temperature increased at a heating rate of 1 °C/min in the DOPE-Me membrane, a direct  $L_{\alpha}$  to  $H_{II}$  phase transition occurred without the formation of the Q<sub>II</sub> phase.<sup>45</sup> This result indicates that  $E_a$  (L<sub>a</sub>  $\rightarrow$  Q<sub>II</sub><sup>D</sup>) of the DOPE-Me membrane is greater than its  $E_a$  ( $L_{\alpha} \rightarrow H_{II}$ ). This is the same as for 20%-DOPS/80%-MO membranes at low pH.

# 5. CONCLUSIONS

In this study, we obtained the values and information on the activation energy of the elementary steps of the low-pHinduced  $L_{\alpha}$  to  $\tilde{Q}_{II}^{D}$  phase transition in 20%-DOPS/80%-MO. The rate constant of the initial step increased with temperature, indicating that the value of  $E_a$  ( $L_{\alpha} \rightarrow H_{II}$ ) does not change with temperature. Its analysis provided the values of  $E_a$  ( $L_{\alpha} \rightarrow H_{II}$ ), which increased with an increase in pH. In contrast, the rate constant of the second step decreased with temperature for pH 2.6, although it increased with temperature at pH 2.7 and 2.8. These results indicate that the value of  $E_a$  ( $H_{II} \rightarrow Q_{II}^{D}$ ) at pH 2.6 increases with temperature, but the values of  $E_a$  ( $H_{II} \rightarrow$  $Q_{II}^{D}$ ) at pH 2.7 and 2.8 are constant with temperature. The values of  $E_a$  ( $H_{II} \rightarrow Q_{II}^{D}$ ) were smaller than those of  $E_a$  ( $L_{\alpha} \rightarrow$  $H_{II}$ ) at the same pH. We analyzed these experimental results of the activation energies using a modified quantitative theory proposed initially by Squires et al.<sup>35</sup> The theory can reasonably explain these results qualitatively.

# ASSOCIATED CONTENT

### **S** Supporting Information

The Supporting Information is available free of charge on the ACS Publications website at DOI: 10.1021/acs.lang-muir.5b03785.

SAXS data of other conditions, waterfall plots of SAXS patterns, temperature dependence of the pH of membrane suspensions, correction of the activation energies based on the temperature-dependent pH shift, and calculation of the water content in each phase (PDF)

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#### Notes

The authors declare no competing financial interest.

# ACKNOWLEDGMENTS

This work was supported in part by a Grant-in-Aid for Scientific Research (B) (no. 15H04361) from the Japan Society for the Promotion of Science (JSPS) to M.Y. Part of this research is based on a Cooperative Research Project of the Research Institute of Electronics, Shizuoka University. The synchrotron radiation experiments were performed using BL40B2 at SPring-8 with the approval of the Japan Synchrotron Radiation Research Institute (JASRI) (proposal nos. 2014A1180, 2014B1240, 2015A1242, and 2015B1208) and BL-6A of the Photon Factory (Tsukuba, Japan) with the approval of the Photon Factory Advisory Committee (proposal no. 2014G016). Preliminary SAXS experiments were performed at the Molecular Structure Analysis Section of Shizuoka University RIGST.

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